

**DIRECTORATE OF DISTANCE & CONTINUING EDUCATION**

**MANONMANIAM SUNDARANAR UNIVERSITY**

**TIRUNELVELI- 627 012**

**OPEN AND DISTANCE LEARNING (ODL) PROGRAMMES**

**(FOR THOSE WHO JOINED THE PROGRAMMES FROM THE ACADEMIC YEAR 2023–2024)**



**M.Sc. Chemistry Course Material**

**PHYSICAL CHEMISTRY - I**

**Course Code SCHM22**

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## PHYSICAL CHEMISTRY-I

**UNIT-I:** Classical Thermodynamics: Partial molar properties, Chemical potential, Gibb's- Duhem equation-binary and ternary systems. Determination of partial molar quantities. Thermodynamics of real gases - Fugacity- determination of fugacity by graphical and equation of state methods-dependence of temperature, pressure and composition. Thermodynamics of ideal and non-ideal binary mixtures, Duhem - Margulus equation applications of ideal and non-ideal mixtures. Activity and activity coefficients-standard states - determination-vapour pressure, EMF and freezing point methods.

**UNIT-II:** Statistical thermodynamics: Introduction of statistical thermodynamics concepts of thermodynamic and mathematical probabilities-distribution of distinguishable and non-distinguishable particles. Assemblies, ensembles, canonical particles. Maxwell - Boltzmann, Fermi Dirac & Bose-Einstein Statistics- comparison and applications. Partition functions-evaluation of translational, vibrational and rotational partition functions for monoatomic, diatomic and polyatomic ideal gases. Thermodynamic functions in terms of partition functions-calculation of equilibrium constants. Statistical approach to Thermodynamic properties: pressure, internal energy, entropy, enthalpy, Gibb's function, Helmholtz function residual entropy, equilibrium constants and equipartition principle. Heat capacity of mono and diatomic gases-ortho and para hydrogen. Heat capacity of solidsEinstein and Debye models.

**UNIT-III:** Irreversible Thermodynamics: Theories of conservation of mass and energy entropy production in open systems by heat, matter and current flow, force and flux concepts. Onsager theory-validity and verification- Onsager reciprocal relationships. Electro kinetic and thermo mechanical effects-Application of irreversible thermodynamics to biological systems.

**UNIT-IV:** Kinetics of Reactions: Theories of reactions-effect of temperature on reaction rates, collision theory of reaction rates, Unimolecular reactions -Lindeman and Christiansen hypothesis molecular beams, collision cross sections, effectiveness of collisions, Potential energy surfaces. Transition state theory-evaluation of thermodynamic parameters of activation-applications of ARRT to reactions between atoms and molecules, time and true order-kinetic parameter evaluation. Factors determine the reaction rates in solution - primary salt effect and secondary salt effect, Homogeneous catalysis- acid- base catalysis-mechanism of acid base catalyzed reactionsBronsted catalysis law, enzyme catalysis-Michelis-Menton catalysis.

**UNIT-V:** Kinetics of complex and fast reactions: Kinetics of complex reactions, reversible reactions, consecutive reactions, parallel reactions, chain reactions. Chain reactions-chain length, kinetics of  $H_2 - Cl_2$  &  $H_2 - Br_2$  reactions (Thermal and Photochemical reactions) - Rice Herzfeld mechanism. Study of fast reactions-relaxation methods- temperature and pressure jump methods electric and magnetic field jump methods stopped flow flash photolysis methods and pulse radiolysis. Kinetics of polymerization-free radical, cationic, anionic polymerization - Polycondensation.

### **Recommended Text**

1. J. Rajaram and J.C. Kuriacose, Thermodynamics for Students of Chemistry, 2nd edition, S.L.N.Chand and Co., Jalandhar, 1986.
2. I.M. Klotz and R.M. Rosenberg, Chemical thermodynamics, 6th edition, W.A. Benjamin Publishers, California, 1972.
3. M.C. Gupta, Statistical Thermodynamics, New Age International, Pvt. Ltd., New Delhi, 1995.
4. K.J. Laidler, Chemical Kinetics, 3rd edition, Pearson, Reprint - 2013.
5. J. Rajaram and J.C. Kuriokose, Kinetics and Mechanisms of chemical transformation, Macmillan India Ltd, Reprint - 2011.

### **Reference Books**

1. D.A. Mcquarrie And J.D. Simon, Physical Chemistry - A Molecular Approach, Viva Books Pvt. Ltd., New Delhi, 1999.
2. R.P. Rastogi and R.R. Misra, Classical Thermodynamics, Vikas Publishing, Pvt. Ltd., New Delhi, 1990.
3. S.H. Maron and J.B. Lando, Fundamentals of Physical Chemistry, Macmillan Publishers, New York, 1974
4. K.B. Ytsimiriski, "Kinetic Methods of Analysis", Pergamom Press, 1996.
5. Gurdeep Raj, Phase rule, Goel Publishing House, 2011.

# Physical Chemistry-I

## Unit-I

### Classical Thermodynamics

Partial molar properties are thermodynamic properties of a mixture that describe the change in a specific property of the mixture when a small amount of one component is added to or removed from the mixture, while keeping the temperature, pressure, and amount of other components constant. These properties are important in the study of solutions and mixtures in chemistry and chemical engineering. Some commonly discussed partial molar properties include:

1. **Partial Molar Volume (V):** The change in volume of a mixture when a small amount of one component is added to it, keeping temperature and pressure constant. Mathematically, it is represented as:

$$V_i = (\partial V / \partial n_i)_{T,P,n_j}$$

Where  $V_i$  is the partial molar volume of component  $i$ ,  $V$  is the total volume of the mixture, and  $n_i$  is the amount of component  $i$ .

2. **Partial Molar Enthalpy (H):** The change in enthalpy of a mixture when a small amount of one component is added to it, keeping temperature, pressure, and the amount of other components constant. Mathematically, it is represented as:

$$H_i = (\partial H / \partial n_i)_{T,P,n_j}$$

Where  $H_i$  is the partial molar enthalpy of component  $i$ ,  $H$  is the total enthalpy of the mixture, and  $n_i$  is the amount of component  $i$ .

3. **Partial Molar Gibbs Free Energy (G):** The change in Gibbs free energy of a mixture when a small amount of one component is added to it, keeping temperature,

pressure, and the amount of other components constant. Mathematically, it is represented as:

$$G_i = (\partial G / \partial n_i)_{T,P,n_j}$$

Where  $G_i$  is the partial molar Gibbs free energy of component  $i$ ,  $G$  is the total Gibbs free energy of the mixture, and  $n_i$  is the amount of component  $i$ .

Partial molar properties are useful in understanding the behavior of solutions and mixtures, particularly in processes such as phase equilibria, chemical reactions, and separations. They provide insights into how the addition or removal of a component affects the overall properties of the mixture.

Determining partial molar quantities involves experimental or theoretical methods to isolate the contribution of a specific component to the overall property of a mixture. Here's how partial molar quantities can be determined:

#### **Experimental Methods:**

#### **1. Partial Molar Volume ( $\bar{V}_iM$ ):**

- **Experimental Methods:** Differential scanning calorimetry (DSC), densimetry, or pycnometry can be used to measure changes in volume upon addition of a component while keeping other variables constant.
- **Calculation:** The change in volume upon adding a small amount of a component ( $\Delta V$ ) divided by the amount of substance added ( $\Delta n_i$ ) gives the partial molar volume ( $\bar{V}_iM$ ).

#### **2. Partial Molar Enthalpy ( $\bar{H}_iM$ ):**

- **Experimental Methods:** Calorimetry techniques such as differential scanning calorimetry (DSC) or isothermal titration calorimetry (ITC) can be used to measure the heat exchanged when adding a component.

- **Calculation:** The heat exchanged ( $q$ ) divided by the amount of substance added ( $\Delta n_i$ ) gives the partial molar enthalpy ( $\bar{H}_i^M$ ).

### 3. Partial Molar Gibbs Free Energy ( $\bar{G}_i^M$ ):

- **Experimental Methods:** For dilute solutions, the Gibbs free energy change can be determined using vapor pressure measurements or osmotic pressure measurements.

- **Calculation:** The change in Gibbs free energy ( $\Delta G$ ) upon adding a small amount of a component, divided by the amount of substance added ( $\Delta \Delta n_i$ ), gives the partial molar Gibbs free energy ( $\bar{G}_i^M$ ).

#### Theoretical Methods:

### 1. Activity Coefficients ( $\gamma_i$ ):

- **Experimental Methods:** Experimental data such as vapor-liquid equilibrium (VLE) or activity coefficient measurements can be used to determine activity coefficients.

- **Calculation:** The ratio of the partial molar property to the property of the pure substance ( $\lim_{x_i \rightarrow 1} x_i$ ) yields the activity coefficient ( $\gamma_i$ ), which is used to calculate the partial molar property.

## 2. Models:

- **Modeling:** Thermodynamic models such as the Margules, Van Laar, or Wilson models can be employed to predict partial molar properties based on experimental data and molecular interactions.

## 3. Computer Simulations:

- **Simulation Methods:** Molecular dynamics (MD) simulations or Monte Carlo simulations can be used to calculate partial molar properties by simulating the behavior of individual molecules within a mixture.

## 4. Derivative Approaches:

- **Mathematical Analysis:** Mathematical derivatives of equations describing the overall properties of the mixture with respect to changes in the amount of a specific component can yield partial molar properties.

In practice, a combination of experimental measurements, theoretical models, and computational simulations is often employed to accurately determine partial molar quantities for various components in a mixture.

### Gibbs-Duhem equation

The Gibbs-Duhem equation is a fundamental relation in thermodynamics that describes the behavior of extensive properties of a thermodynamic system. It states that for any mixture of chemical substances at equilibrium, there exists a linear relationship between changes in the intensive properties of the system.



Let's start with the expression of the Gibbs free energy  $G$  for a system of constant temperature and pressure:

$$G = H - TS$$

Where:

- $G$  is the Gibbs free energy
- $H$  is the enthalpy
- $T$  is the temperature
- $S$  is the entropy

For a system containing  $N$  moles of substances, we can express  $G$  in terms of the chemical potential  $\mu_i$  for each component:

$$G = \sum_{i=1}^N \mu_i n_i$$

Where:

- $\mu_i$  is the chemical potential of component  $i$
- $n_i$  is the number of moles of component  $i$

Using the definition of chemical potential:

$$\mu_i = \left(\frac{\partial G}{\partial n_i}\right)_{T,P}$$

Now, differentiate the Gibbs free energy expression with respect to the number of  $n_i$ :

$$dG = \sum_{i=1}^N \left(\frac{\partial \mu_i}{\partial n_i}\right)_{T,P} dn_i + \sum_{i=1}^N \mu_i dn_i$$

Since the total number of moles is constant,  $\sum_{i=1}^N dn_i = 0$ , so we have:

$$\sum_{i=1}^N dn_i = 0$$

$$dG = \sum_{i=1} (\partial\mu_i/\partial n_i)_{T,P} dn_i$$

Now, recall that for an ideal mixture, the chemical potential  $\mu_i$  of each component depends only on the concentration of that component, not on the concentrations of the other components. Therefore:

$$\partial\mu_i/\partial n_i = (\partial\mu_i/\partial x_i)_{T,P}$$

Where  $x_i$  is the mole fraction of component  $i$ . So we can rewrite the equation as:

$$dG = \sum_{i=1} (\partial\mu_i/\partial x_i)_{T,P} dx_i$$

Now, let's define the partial molar Gibbs free energy  $G_i$  as:

$$G_i = (\partial G / \partial n_i)_{T,P}$$

Therefore, we have:

$$dG = \sum_{i=1} G_i dn_i$$

And using the definition of mole fraction  $x_i$  as:

$$x_i = n_i / \sum_{i=1} n_i$$

We can rewrite the expression for  $dn_i$  as:

$$dn_i = n dx_i + x_i dn$$

Substituting this into the equation for  $dG$ , we get:

$$dG = \sum_{i=1}^n G_i (n dx_i + x_i dn)$$

$$dG = n \sum_{i=1}^n G_i dx_i + \sum_{i=1}^n x_i G_i dn$$

$$dG = n \sum_{i=1}^n G_i dx_i + \sum_{i=1}^n x_i \mu_i dn$$

Now, recall the definition of the chemical potential  $\mu_i$ :

$$\mu_i = G_i + RT \ln x_i$$

Substitute this into the equation:

$$dG = \sum_{i=1}^n G_i dx_i + \sum_{i=1}^n x_i (G_i + RT \ln x_i) dn$$

$$dG = n \sum_{i=1}^n G_i dx_i + \sum_{i=1}^n x_i G_i dn + RT \sum_{i=1}^n x_i \ln x_i dn$$

Since  $\sum_{i=1}^n x_i dn = dn$ , we have:

$$dG = n \sum_{i=1}^n G_i dx_i + \sum_{i=1}^n x_i G_i dn + RT dn \sum_{i=1}^n x_i \ln x_i$$

$$dG = n \sum_{i=1}^n G_i dx_i + \sum_{i=1}^n x_i \ln x_i$$

$$dG = \sum_{i=1}^n (G_i + RT \ln x_i) dx_i$$

$$dG = \sum_{i=1} \mu_i dx_i$$

Therefore, the Gibbs-Duhem equation is:

$$\sum_{i=1} \mu_i dx_i = 0$$

This equation states that for any mixture of chemical substances at equilibrium, there exists a linear relationship between changes in the intensive properties of the system.

### **Fugacity:**

Fugacity is a concept in thermodynamics and statistical mechanics that represents an effective measure of the escaping tendency or escaping tendency per particle of a substance from a non-ideal mixture or solution. It is often denoted by the symbol  $f$  or  $f_i$  for a specific component  $i$  in a mixture. Fugacity is particularly useful in describing non-ideal gases and solutions, where the pressure or concentration does not directly correspond to the escaping tendency of the substance.

**Escape Tendency:** Fugacity represents the escaping tendency of a substance from a mixture or solution. It accounts for deviations from ideal behavior due to interactions between molecules or particles.

**Non-Ideal Systems:** In non-ideal systems, the fugacity of a component may differ from its partial pressure or concentration. This is because the activity coefficient, which reflects the deviation from ideal behavior, modifies the fugacity.

**Relation to Pressure and Chemical Potential:** In an ideal gas or solution, fugacity is equal to pressure or chemical potential. However, in non-ideal systems, the

relationship between fugacity, pressure, and chemical potential becomes more complex and is governed by equations such as the Van der Waals equation or activity models.

**Fugacity Coefficient:** In some contexts, especially in thermodynamics, the fugacity coefficient ( $\phi$ ) is used. It relates the fugacity of a substance to its ideal pressure or concentration. For an ideal gas or solution, the fugacity coefficient is equal to 1.

**Units:** Fugacity has the same units as pressure (e.g., pascals, atmospheres) or concentration (e.g., moles per cubic meter).

**Calculation:** Fugacity can be calculated using various equations of state or activity models, depending on the nature of the system and the level of approximation required.

#### **Importance of Fugacity:**

- Fugacity plays a crucial role in understanding and predicting the behavior of non-ideal systems, including phase equilibria, chemical reactions, and separation processes.
- It is particularly relevant in industries such as chemical engineering, where accurate predictions of thermodynamic properties are essential for process design and optimization.

Overall, fugacity provides a more accurate description of the escaping tendency of substances in non-ideal systems compared to pressure or concentration alone, making it a valuable concept in thermodynamics and statistical mechanics.

Measuring fugacity directly can be challenging because it is a concept used to describe the escaping tendency of a substance from a non-ideal mixture or solution,

rather than a directly measurable quantity. However, there are indirect methods and techniques used to estimate or infer fugacity in various experimental settings. Here are some approaches:

### **1. Equations of State (EOS):**

- Fugacity can be calculated using equations of state such as the Van der Waals equation, Redlich-Kwong equation, or Peng-Robinson equation. These equations relate fugacity to pressure, volume, temperature, and the properties of the substance.
- Experimental data, such as pressure-volume-temperature (PVT) measurements, can be used to fit parameters in these equations, allowing for the determination of fugacity.

### **2. Activity Coefficients:**

- In the context of solutions, fugacity can be related to activity coefficients through activity models such as the Van Laar equation, Wilson equation, or NRTL equation. These models describe deviations from ideal behavior in terms of activity coefficients, which affect the fugacity of each component.
- Experimental measurements of vapor-liquid equilibria (VLE) or osmotic pressure can be used to determine activity coefficients, which can then be used to calculate fugacity.

### **3. Phase Equilibrium Measurements:**

- Phase equilibrium experiments, such as vapor-liquid equilibrium (VLE) measurements or liquid-liquid equilibrium (LLE) measurements, provide valuable data for estimating fugacity.
- By measuring the composition of phases in equilibrium and applying phase equilibrium models, fugacity coefficients and fugacities can be estimated.

### **4. Empirical Correlations:**

- Empirical correlations based on experimental data or theoretical models can provide estimates of fugacity in specific systems or conditions.
- These correlations may be based on regression analysis of experimental data or derived from theoretical considerations.

### 5. Theoretical Models:

- Quantum chemical calculations or molecular simulations can provide insights into intermolecular interactions and their effects on fugacity.
- Computational methods such as density functional theory (DFT) or Monte Carlo simulations can be used to predict fugacity in complex systems.

### Ternary Systems

Ternary phase diagrams are graphical representations used to understand the behavior of a system composed of three components. These diagrams are commonly used in materials science, chemistry, and metallurgy to depict the phase relationships between the components at various combinations of temperature, pressure, and composition.

Here's a general explanation of how ternary phase diagrams work and what they depict:

1. **Components:** A ternary phase diagram represents a system composed of three components. These components could be elements, compounds, or mixtures.
2. **Axes:** Ternary phase diagrams typically have three axes. Each axis represents the composition of one of the components. These compositions are usually expressed as fractions or percentages of the total.

3. **Phases:** The different phases of the system, such as solid, liquid, and gas, are represented within the diagram. Boundaries between these phases are shown as lines or curves.
4. **Phase Regions:** Each area within the diagram represents a different phase or combination of phases that exist under specific conditions of temperature, pressure, and composition.
5. **Phase Boundaries:** Phase boundaries indicate the conditions under which two phases coexist in equilibrium. These boundaries can include solid-solid, liquid-liquid, solid-liquid, etc.
6. **Tie Lines:** Tie lines are lines drawn between two points within a phase region. They indicate the compositions of the coexisting phases at equilibrium.
7. **Invariant Reactions:** Points where three phase boundaries intersect are known as invariant points. At these points, three phases coexist in equilibrium.
8. **Solid Solutions:** Ternary phase diagrams can also depict solid solutions, where different components are dissolved in each other in the solid state.
9. **Eutectic Points:** In some ternary phase diagrams, eutectic points may exist. These are points where a mixture of three components melts at the lowest possible temperature.

When interpreting a ternary phase diagram, it's essential to understand the behavior of the system under different conditions and how changes in temperature, pressure, or composition affect the phase relationships. Additionally, experimental data and theoretical models are often used to construct and interpret ternary phase diagrams accurately.

- Each apex represents one component of the system (A, B, and C).
- The sides connecting the apexes represent binary phase boundaries between pairs of components.



- The central region represents the ternary phase space, where all three components coexist.
- The lines and curves within the diagram represent phase boundaries and tie lines, indicating regions of phase equilibrium and phase compositions.
- The symbols inside the phase regions indicate the phases present in those regions (e.g., liquid, solid, gas).

Please note that the actual appearance and details of a ternary phase diagram can vary significantly based on the specific properties and interactions of the components involved. Real-world ternary phase diagrams are often more complex and may require professional software or experimental data to construct accurately.

## Thermodynamics of ideal and non-ideal binary systems

### Ideal Binary Systems:

An ideal binary system is a theoretical concept that simplifies the analysis of mixtures. In an ideal binary system:

1. **No Interactions Between Molecules:** Molecules of different components do not interact with each other, meaning there are no attractive or repulsive forces between them.
2. **Mixing is Energetically Neutral:** Mixing of the components does not result in any energy changes.
3. **Raoult's Law Applies:** Raoult's law states that the partial vapor pressure of each component in the mixture is directly proportional to its mole fraction in the liquid phase and the vapor pressure of the pure component. Mathematically, for an ideal binary mixture:

$$P_i = x_i P_i^*$$

Where:

- $P_i$  is the partial pressure of component  $i$  in the mixture.
  - $x_i$  is the mole fraction of component  $i$  in the liquid phase.
  - $P_i^*$  is the vapor pressure of pure component  $i$ .
4. **Ideal Behavior is Observed at All Compositions and Temperatures:** This means that the behavior of the mixture is predicted perfectly by Raoult's law.

### Non-Ideal Binary Systems:

Non-ideal binary systems exhibit deviations from ideal behavior due to molecular interactions between different components. There are two types of deviations:

1. **Positive Deviation:** In a positive deviation from Raoult's law, the observed vapor pressure of the mixture is higher than predicted by Raoult's law. This typically occurs when molecules in the mixture have stronger attractions for each other than for themselves. It often happens in mixtures containing dissimilar molecules.
2. **Negative Deviation:** In a negative deviation, the observed vapor pressure of the mixture is lower than predicted by Raoult's law. This occurs when the intermolecular attractions between different molecules are weaker than those within individual pure components. This often occurs in mixtures where components are similar in nature.

### Thermodynamics of Non-Ideal Binary Systems:

1. **Gibbs Free Energy:** For non-ideal mixtures, the Gibbs free energy ( $G$ ) of mixing differs from ideal behavior. The excess Gibbs free energy ( $G^E$ ) is introduced to account for this difference. For a binary mixture:

$$G = G_{\text{ideal}} + G^E$$

2. **Activity Coefficients:** Activity coefficients ( $\gamma_i$ ) are introduced to quantify deviations from ideal behavior. They are defined as:

$$\mu_i = \mu_i^{\text{ideal}} + RT \ln \gamma_i$$

Where:

- $\mu_i$  is the chemical potential of component  $i$ .
- $\mu_i^{\text{ideal}}$  is the chemical potential of component  $i$  in an ideal solution.
- $\gamma_i$  is the activity coefficient of component  $i$ .

3. **Phase Equilibria:** Non-ideal mixtures may exhibit different phase behaviors compared to ideal mixtures. Phase diagrams for non-ideal mixtures may show azeotropes or immiscibility regions, which are not observed in ideal mixtures.

4. **Activity Models:** Various activity models, such as Margules, Van Laar, and Wilson models, are used to correlate and predict activity coefficients for non-ideal mixtures based on experimental data.

Henry's Law describes the solubility of a gas in a liquid at a constant temperature, under conditions where the gas does not react chemically with the solvent. It states that the concentration of a gas dissolved in a liquid is directly proportional to the partial pressure of that gas above the liquid. This law is typically expressed mathematically as:

$$C = k_H \cdot P$$

Where:

- $C$  is the concentration of the gas in the liquid (typically in units of mol/L or Molarity).
- $k_H$  is Henry's law constant, which is specific to the gas-solvent system and temperature (units of M/atm or M/Pa).
- $P$  is the partial pressure of the gas above the liquid (in units of atm or Pa).

For an ideal binary system, Henry's Law can be applied to each component separately. Let's consider a binary system consisting of components A and B, where A is the gas being dissolved in the liquid solvent:

For component A:

$$C_A = k_{HA} \cdot P_A$$

And for component B:

$$C_B = k_{HB} \cdot P_B$$

Where:

- $C_A$  and  $C_B$  are the concentrations of components A and B in the liquid respectively.
- $k_{HA}$  and  $k_{HB}$  are the Henry's law constants for components A and B respectively.
- $P_A$  and  $P_B$  are the partial pressures of components A and B above the liquid respectively.

In an ideal binary system, the behavior of the components is independent of each other, so each component follows Henry's Law independently. This implies that the solubility of each gas in the liquid is directly proportional to its own partial pressure and governed by its respective Henry's law constant.

It's important to note that Henry's Law is an approximation that holds well for dilute solutions and low to moderate pressures. For highly concentrated solutions or high pressures, deviations from Henry's Law behavior may occur, especially in non-ideal systems.

**Activity and Activity Coefficients:**

1. **Activity:** In thermodynamics, activity ( $a$ ) is a measure of the "effective concentration" of a species in a mixture, accounting for deviations from ideal behavior due to interactions between molecules. It is defined as the ratio of the chemical potential of a component in a mixture to its chemical potential in a reference state.

$$a_i = \mu_i / \mu_i^0$$

2. **Activity Coefficient:** The activity coefficient ( $\gamma_i$ ) quantifies the deviation from ideal behavior in a solution. It is defined as the ratio of the activity of a species to its concentration in a solution at a given condition.

$$\gamma_i = a_i / C_i$$

### Standard States:

In thermodynamics, a standard state is a defined reference state used for specifying properties such as pressure, temperature, concentration, etc., which allows for consistency and comparability of measurements. Commonly used standard states include:

- For gases: 1 atm pressure and a specified temperature (e.g., 25°C or 298 K).
- For liquids and solids: Pure substance at a specified pressure and temperature.
- For solutions: An infinitely diluted solution (infinite dilution) under specified conditions.

### Determination of Activity and Activity Coefficients:

1. **Vapor Pressure Method:** In this method, the activity coefficients of components in a liquid mixture are determined by comparing the vapor pressures of the components in the mixture to those in their pure states using Raoult's law or other vapor pressure equations.

2. **Electromotive Force (EMF) Method:** Also known as the electromotive force measurement method or cell method, this technique measures the potential difference between electrodes in an electrochemical cell containing the solution of interest. It is used primarily for determining activity coefficients of ions in electrolyte solutions.
3. **Freezing Point Depression Method:** This method involves measuring the depression in the freezing point of a solvent when a solute is dissolved in it. By comparing the observed freezing point depression to the theoretical value predicted by the ideal behavior, activity coefficients of the solute can be determined.

#### **Significance:**

- **Process Design:** Understanding activity and activity coefficients is crucial for the design and optimization of chemical processes involving mixtures, such as distillation, extraction, and crystallization.
- **Equilibrium Calculations:** Activity coefficients are essential for accurate predictions of phase equilibria, chemical reactions, and other thermodynamic properties in non-ideal systems.
- **Correlation and Prediction:** Experimental data on activity coefficients are often used to develop thermodynamic models that can correlate and predict the behavior of complex mixtures under various conditions.

#### **Vapour pressure method**

The vapour pressure method is a common experimental technique used to determine the activity coefficients of components in a liquid mixture. This method involves measuring the vapor pressures of the components in the mixture and comparing them to the vapor pressures of the pure components at the same temperature. From these measurements, activity coefficients can be calculated using Raoult's law or other vapor pressure equations.

Here's a general outline of the experimental procedure for the vapor pressure method:

### **Equipment and Materials:**

1. **Refrigerated Circulator:** To maintain a constant temperature.
2. **Pressure Transducer or Manometer:** To measure vapor pressures.
3. **Temperature Probe or Thermometer:** To monitor temperature.
4. **Glass Apparatus:** Such as a vapor pressure apparatus or a vapor-liquid equilibrium (VLE) setup.
5. **Pure Samples of Components:** Needed for comparison.
6. **Analytical Balance:** To measure sample quantities accurately.
7. **Vacuum Pump:** To evacuate the system and create a vacuum.

### **Procedure:**

#### **1. Preparation of Apparatus:**

- Clean all glassware thoroughly to avoid contamination.
- Assemble the vapor pressure apparatus or VLE setup according to the manufacturer's instructions.
- Connect the pressure transducer or manometer to the system to measure vapor pressures.

#### **2. Calibration:**

- Calibrate the pressure transducer or manometer using known reference pressures.
- Ensure that the temperature probe or thermometer is accurate and calibrated.

#### **3. Sample Preparation:**

- Weigh accurately measured quantities of each component of the liquid mixture.

- Place the samples in separate containers or compartments within the vapor pressure apparatus.

#### 4. **Evacuation:**

- Evacuate the system using the vacuum pump to remove any air or impurities.
- Ensure that the system is sealed to prevent leaks.

#### 5. **Temperature Control:**

- Start the refrigerated circulator and set it to the desired temperature.
- Monitor and maintain a constant temperature throughout the experiment.

#### 6. **Measurement:**

- Once the system reaches the desired temperature, record the vapor pressures of the components in the mixture using the pressure transducer or manometer.
- Repeat the measurements for different compositions of the mixture by varying the proportions of the components.

#### 7. **Comparison:**

- Compare the vapor pressures of the components in the mixture to the vapor pressures of the pure components at the same temperature.
- Calculate the activity coefficients using appropriate equations, such as Raoult's law or other vapor pressure equations.

#### 8. **Analysis:**

- Analyze the data and plot graphs of vapor pressure versus composition.
- Use the experimental data to determine the activity coefficients of the components in the mixture.

#### 9. **Cleanup:**

- Clean and dismantle the apparatus after the experiment.
- Dispose of any waste materials properly.

#### **Data Analysis:**



- Calculate the activity coefficients using the measured vapor pressures and known vapor pressures of the pure components.
- Use appropriate equations or models, such as Raoult's law, to determine the activity coefficients.
- Plot graphs of vapor pressure versus composition and analyze the data to verify the behavior of the mixture.

#### **Precautions:**

- Ensure that the system is properly sealed to prevent leaks.
- Handle chemicals with care and follow safety procedures.
- Maintain a constant temperature throughout the experiment.
- Calibrate all instruments and equipment accurately.

By following these steps and precautions, the vapor pressure method can provide valuable data for determining the activity coefficients of components in a liquid mixture

#### **Freezing point method**

The determination of activity and activity coefficients using the freezing point depression method involves measuring the depression in the freezing point of a solvent caused by the presence of a solute. This method is particularly useful for dilute solutions and relies on the relationship between the concentration of the solute and the freezing point depression, as described by the equation:

$$\Delta T_f = K_f m$$

Where:

- $\Delta T_f$  is the freezing point depression,
- $K_f$  is the cryoscopic constant of the solvent,
- $m$  is the molality of the solute.

**Procedure:**

**1. Preparation of Solutions:**

- Prepare a series of solutions with known concentrations of the solute. These solutions should cover a range of concentrations, typically spanning from very dilute to moderately concentrated.
- Accurately measure the masses of solute and solvent needed to prepare each solution.

**2. Determination of Freezing Points:**

- Use a suitable apparatus, such as a Beckmann or freezing point depression apparatus, to measure the freezing points of the prepared solutions.
- Calibrate the apparatus according to the manufacturer's instructions.
- Record the freezing points of each solution.

**3. Calculation of Freezing Point Depression:**

- Calculate the freezing point depression ( $\Delta T_f$ ) for each solution by subtracting the freezing point of the pure solvent from the freezing point of the solution.
- Ensure that the measurements are accurate and consistent.

**4. Plotting the Depression vs. Molality:**

- Plot a graph of freezing point depression ( $\Delta T_f$ ) versus molality ( $m$ ) for the solutions.
- The resulting curve should be linear for dilute solutions according to the equation  $\Delta T_f = K_f \cdot m$ .
- Note any deviations from linearity, which may indicate non-ideal behavior.

**5. Determination of Activity Coefficients:**

- The cryoscopic constant ( $K_f$ ) of the solvent is known. By plotting  $\Delta T_f$  versus  $m$ , you can determine the slope of the line, which corresponds to  $K_f$ .

- From the slope and known concentration of the solute, calculate the activity coefficients using the equation:  $\gamma = 1 - K_f \cdot m \Delta T_f$

### Analysis and Interpretation:

- **Ideal Behavior:** In ideal solutions, the freezing point depression is directly proportional to the molality of the solute, and the plot of  $\Delta T_f$  versus  $m$  yields a straight line passing through the origin.
- **Non-Ideal Behavior:** Deviations from linearity indicate non-ideal behavior. These deviations can be attributed to interactions between solute and solvent molecules and are quantified by activity coefficients.
- **Activity Coefficients:** Activity coefficients can be determined from the slopes of the curves and are crucial for understanding the extent of non-ideality in the solution.

### Considerations and Precautions:

- Ensure accurate measurements of masses, temperatures, and freezing points.
- Use a suitable solvent with a well-known cryoscopic constant.
- Consider the limitations of the freezing point depression method for concentrated solutions and systems exhibiting phase separation.
- Verify the linearity of the depression vs. molality plot for dilute solutions.

By following these steps and considerations, the freezing point depression method provides a valuable means of determining activity and activity coefficients in solution systems.

### Derivation of Duhem-Margules equation

The Duhem-Margules equation is a relation used to describe the excess Gibbs free energy of mixing for non-ideal liquid solutions. It is an empirical equation derived from the concept of activity coefficients in binary liquid mixtures. The equation is given by:

$$\Delta G_{\text{mix}} / RT = x_1 x_2 (A_{21} + A_{12})$$

Where:

- $\Delta G_{\text{mix}}$  is the excess Gibbs free energy of mixing per mole of mixture.
- $R$  is the universal gas constant.
- $T$  is the temperature.
- $x_1$  and  $x_2$  are the mole fractions of components 1 and 2, respectively.
- $A_{21}$  and  $A_{12}$  are the Margules parameters.

Now, let's derive the Duhem-Margules equation:

### Derivation:

Starting with the Gibbs-Duhem equation for a binary system:

$$x_1 d\mu_1 + x_2 d\mu_2 = 0$$

Where  $\mu_1$  and  $\mu_2$  are the chemical potentials of components 1 and 2, respectively.

From thermodynamic principles, the chemical potential  $\mu_i$  can be expressed as:

$$\mu_i = \mu_i^{\text{ideal}} + RT \ln \gamma_i$$

Where  $\mu_i^{\text{ideal}}$  is the chemical potential of component  $i$  in an ideal solution,  $\gamma_i$  is the activity coefficient of component  $i$ , and  $R$  and  $T$  have their usual meanings.

Substituting these expressions into the Gibbs-Duhem equation, we get:

$$x_1 d(\mu_1^{\text{ideal}} + RT \ln \gamma_1) + x_2 d(\mu_2^{\text{ideal}} + RT \ln \gamma_2) = 0$$

Now, expanding and rearranging terms:

$$x_1 d\mu_1^{\text{ideal}} + x_1 RT d \ln \gamma_1 + x_2 d\mu_2^{\text{ideal}} + x_2 RT d \ln \gamma_2 = 0$$

Since the activity coefficient  $\gamma_i$  is assumed to depend only on the composition, we can write:

$$d \ln \gamma_1 = 1/x_1 (\partial \ln \gamma_1 / \partial x_1)_{T,P} dx_1$$

$$d \ln \gamma_2 = 1/x_2 (\partial \ln \gamma_2 / \partial x_2)_{T,P} dx_2$$

Substituting these expressions back into the equation, we get:

$$x_1 d\mu_1^{\text{ideal}} + x_1 RT 1/x_1 (\partial \ln \gamma_1 / \partial x_1)_{T,P} dx_1 + x_2 d\mu_2^{\text{ideal}} + x_2 RT 1/x_2 (\partial \ln \gamma_2 / \partial x_2)_{T,P} dx_2 = 0$$

Now, the chemical potentials ideal  $\mu_i^{\text{ideal}}$  are related to the partial molar Gibbs free energies  $G_i$  as:

$$\mu_i^{\text{ideal}} = (\partial G / \partial n_i)_{T,P} = G_i$$

Substituting this into the equation and dividing throughout by  $RT$ , we get:

$$x_1 dG_1/RT + (\partial \ln \gamma_1 / \partial x_1)_{T,P} dx_1 + x_2 dG_2/RT + (\partial \ln \gamma_2 / \partial x_2)_{T,P} dx_2 = 0$$

Now, define  $A_{12}$  and  $A_{21}$  as follows:

$$A_{12} = - 1/RT (\partial \ln \gamma_1 / \partial x_1)_{T,P}$$

$$A_{21} = - 1/RT (\partial \ln \gamma_2 / \partial x_2)_{T,P}$$

Substituting these expressions into the equation, we get:

$$x_1 dG_1/RT + x_1 A_{12} dx_1 + x_2 dG_2/RT + x_2 A_{21} dx_2 = 0$$

Now,  $dG_i / RT = d(\Delta G_i^E / RT) / RT = d\Delta G_i^E / RT^2$

where  $\Delta G_i^E$  is the excess Gibbs free energy of component  $i$ .

So, we have:

$$x_1 d\Delta G_1^E / RT^2 + x_2 d\Delta G_2^E / RT^2 + x_1 A_{12} dx_1 + x_2 A_{21} dx_2 = 0$$

Rearranging terms, we obtain:

$$x_1 dx_1 + x_2 dx_2 + (A_{12} + A_{21}) x_1 x_2 dx_1 = 0$$

$$(1 + (A_{12} + A_{21}) x_2) dx_1 + (1 + (A_{12} + A_{21}) x_1) dx_2 = 0$$

Now, integrate both sides of the equation:

$$\int (1 + (A_{12} + A_{21}) x_2) dx_1 + \int (1 + (A_{12} + A_{21}) x_1) dx_2 = 0$$

$$x_1 + (A_{12} + A_{21}) x_1 x_2 = C_1$$

$$x_2 + (A_{12} + A_{21}) x_1 x_2 = C_2$$

Where  $C_1$  and  $C_2$  are constants of integration.

Now, let's define  $\Delta G_{\text{mix}}$  as:

$$\Delta G_{\text{mix}} = G - G_{\text{ideal}} = RT \ln \gamma_1 + RT \ln \gamma_2$$

$$\Delta G_{\text{mix}} = RT \ln \gamma_1 + RT \ln \gamma_2 = RT \ln(\gamma_1 \gamma_2)$$

$$\Delta G_{\text{mix}} = RT \ln(\gamma_1 \gamma_2) = RT \ln(1 + (A_{12} + A_{21}) x_1 x_2)$$

$$\Delta G_{\text{mix}} / RT = \ln(1 + (A_{12} + A_{21}) x_1 x_2)$$

Now, we can use the approximation  $\ln(1+x) \approx x$  for small values of  $x$  to simplify the equation:

$$\Delta G_{\text{mix}} / RT \approx (A_{12} + A_{21})x_1x_2$$

Hence, we arrive at the Duhem-Margules equation:

$$\Delta G_{\text{mix}} / RT = (A_{12} + A_{21})x_1x_2$$

This equation describes the excess Gibbs free energy of mixing for a non-ideal binary liquid solution in terms of the Margules parameters  $A_{12}$  and  $A_{21}$ .

## **Unit-2**

### **Statistical Thermodynamics**

Statistical thermodynamics is a branch of thermodynamics that deals with the statistical behavior of a large number of particles in a system. It aims to bridge the

gap between the microscopic properties of individual particles and the macroscopic properties of the system as a whole, such as temperature, pressure, and entropy.

Statistical thermodynamics is based on the principles of probability theory and statistical analysis, and it plays a fundamental role in explaining phenomena observed in classical and quantum mechanical systems.

Statistical thermodynamics provides a microscopic foundation for classical thermodynamics and helps explain the macroscopic behavior of systems.

It is used to study a wide range of physical phenomena, including phase transitions, equilibrium properties of gases, liquids, and solids, chemical reactions, and the behavior of complex materials.

Statistical mechanics is essential for understanding the behavior of systems at the molecular and atomic level and has applications in various fields such as chemistry, physics, materials science, and biology.

Here are some basic terminologies commonly used in statistical thermodynamics:

1. **Ensemble:** A collection of multiple copies of a system, each in different states but sharing the same macroscopic properties like temperature, pressure, and volume.
2. **Microstate:** A specific configuration of the individual particles (atoms or molecules) in a system that fully specifies its state. For example, in a gas, the positions and velocities of all the particles at a particular instant define a microstate.
3. **Macrostate:** A set of macroscopic parameters that describe the overall properties of a system, such as temperature, pressure, volume, and energy.



4. **Probability Distribution:** The distribution of probabilities of finding the system in different microstates, which depends on the macroscopic conditions of the system.

5. **Partition Function ( $Z$ ):** A fundamental quantity in statistical mechanics that encapsulates all the information about the system's microscopic states. It is defined as the sum or integral over all possible states of the Boltzmann factor  $e^{-\beta E_i}$ , where  $E_i$  is the energy of state  $i$  and  $\beta = 1/(kT)$  (where  $k$  is the Boltzmann constant and  $T$  is the temperature).

6. **Boltzmann Distribution:** Describes the distribution of particles over different energy levels in a system at thermal equilibrium. It states that the probability  $P_i$  of finding a particle in a particular energy state  $E_i$  is proportional to  $e^{-\beta E_i}$ , where  $\beta$  is the inverse temperature.

7. **Entropy ( $S$ ):** A measure of the disorder or randomness of a system. In statistical thermodynamics, entropy is related to the number of microstates associated with a given macrostate.

8. **Free Energy:** A thermodynamic potential that measures the maximum amount of reversible work that can be extracted from a system at constant temperature and volume. In statistical mechanics, free energy is often expressed in terms of the partition function.

In statistical thermodynamics, an ensemble is a collection of multiple copies of a system, each in different states but sharing the same macroscopic properties like temperature, pressure, and volume. Ensembles provide a framework for understanding the statistical behavior of systems with a large number of particles. There are several types of ensembles, each corresponding to different conditions

under which the system is studied. Below are the main types of ensembles along with explanations and diagrams:

**Canonical Ensemble:** An ensemble in statistical mechanics that describes a system in thermal equilibrium with a heat reservoir at constant temperature and volume.

**Grand Canonical Ensemble:** An ensemble in statistical mechanics that describes a system in thermal and diffusive equilibrium with a heat reservoir and a particle reservoir at constant temperature, volume, and chemical potential.

These are just a few basic terminologies in statistical thermodynamics, and the field involves many more concepts and terms as one delves deeper into the subject.

### 1. Microcanonical Ensemble:

In the microcanonical ensemble, the system is isolated, meaning it does not exchange energy or particles with its surroundings. The system is described by a fixed total energy  $E$ , volume  $V$ , and number of particles  $N$ .

### 2. Canonical Ensemble:

In the canonical ensemble, the system is in contact with a heat reservoir at constant temperature  $T$ , but it cannot exchange energy or particles with the surroundings. The system is described by its energy  $E$ , volume  $V$ , and number of particles  $N$ , with the total energy allowed to fluctuate.

### 3. Grand Canonical Ensemble:

In the grand canonical ensemble, the system is in contact with a heat reservoir and a particle reservoir, allowing both energy and particles to exchange with the

surroundings. The system is described by its chemical potential  $\mu$ , temperature  $T$ , and volume  $V$ , with both energy and number of particles allowed to fluctuate.

### **Explanation:**

- Each ensemble represents a different set of constraints on the system, such as fixed energy, temperature, or chemical potential.
- Ensembles allow us to compute thermodynamic properties by averaging over all possible states of the system consistent with the constraints of the ensemble.
- The choice of ensemble depends on the experimental conditions and the properties of interest.

Ensembles play a crucial role in statistical thermodynamics, providing a framework for understanding the behavior of systems with many particles. By considering different ensembles, we can analyze systems under various conditions and compute thermodynamic properties relevant to different experimental setups.

The derivation of the Maxwell-Boltzmann distribution involves considering the statistical mechanics of a gas of non-interacting particles in thermal equilibrium. Here's a simplified derivation:

Mathematical probability and thermodynamic probability, while sharing some common concepts, operate within different frameworks and contexts. Let's explore each of them along with examples.

### **Mathematical Probability:**

**Definition:** Mathematical probability deals with the likelihood of an event occurring in a well-defined, non-physical setting. It is expressed as a number between 0 and 1, where 0 indicates impossibility and 1 indicates certainty.

**Concepts:**

1. **Sample Space ( $\Omega$ ):** The set of all possible outcomes of an experiment.
2. **Event (E):** A subset of the sample space, representing a collection of outcomes.
3. **Probability (P):** A function that assigns a numerical value to each event, representing the likelihood of that event occurring.

**Example:** Consider rolling a fair six-sided die. The sample space consists of six possible outcomes: {1, 2, 3, 4, 5, 6}. The probability of rolling a 3 is  $P(3) = \frac{1}{6}$ , assuming the die is fair.

**Thermodynamic Probability:**

**Definition:** Thermodynamic probability, also known as statistical mechanics, deals with the likelihood of different microscopic states of a physical system given its macroscopic properties. It is used to describe the behavior of systems consisting of a large number of particles, such as gases, liquids, and solids.

**Concepts:**

1. **Microstate:** A complete specification of the positions and momenta of all particles in a system at a given instant.
2. **Macrostate:** A description of the system in terms of its macroscopic properties, such as temperature, pressure, volume, and energy.

3. **Boltzmann Distribution:** Describes the probability distribution of particles among different energy states in a system at thermal equilibrium.

**Example:** Consider a system of gas molecules in a box. The macrostate of the system may be described by its temperature, volume, and pressure. The thermodynamic probability gives the likelihood of finding the system in a particular macrostate given its energy distribution among the molecules.

**Comparison:**

- **Scope:** Mathematical probability applies to abstract, well-defined scenarios, while thermodynamic probability applies to physical systems governed by statistical mechanics.
- **Nature of Events:** In mathematical probability, events are discrete and clearly defined, while in thermodynamic probability, events correspond to the distribution of energy states among particles in a system.
- **Applications:** Mathematical probability is widely used in fields such as gambling, statistics, and decision-making. Thermodynamic probability is essential for understanding the behavior of physical systems in statistical mechanics, such as gas laws, phase transitions, and chemical kinetics.

**Distribution of particles**

The distribution of particles, whether distinguishable or non-distinguishable, plays a significant role in various fields such as statistical mechanics, quantum mechanics, and combinatorics. Let's explore the distribution of both types of particles:

### **Distinguishable Particles:**

Distinguishable particles are those that can be uniquely identified from one another. Each particle has its own distinct properties, such as position, momentum, or energy.

#### **1. Classical Particles:**

- In classical statistical mechanics, distinguishable particles are treated as separate entities.
- The distribution of distinguishable particles follows classical statistics, where each particle can occupy its own distinct state without restriction.
- For example, consider a box containing distinguishable classical particles. Each particle can occupy a unique position and momentum within the box.

#### **2. Quantum Particles:**

- In quantum mechanics, distinguishable particles are also treated as separate entities with unique quantum states.
- The distribution of distinguishable quantum particles follows quantum statistics, such as Maxwell-Boltzmann statistics for non-interacting particles or Fermi-Dirac/Bose-Einstein statistics for interacting particles with integer/half-integer spin.
- For example, consider a system of non-interacting particles, such as photons, where each photon can occupy its own quantum state described by its energy and momentum.

### **Non-Distinguishable Particles:**

Non-distinguishable particles are identical and indistinguishable from one another. They cannot be uniquely identified based on their properties alone.

#### **1. Classical Particles:**

- In classical statistical mechanics, non-distinguishable particles are treated as identical entities.
- The distribution of non-distinguishable particles follows classical statistics, but with the constraint that the particles are indistinguishable.
- For example, consider a box containing identical classical particles, such as ideal gas particles. Due to their indistinguishability, the particles cannot be uniquely labeled, and their positions and momenta are treated as exchangeable.

## **2. Quantum Particles:**

- In quantum mechanics, non-distinguishable particles are governed by quantum statistics, which account for their indistinguishability.
- The distribution of non-distinguishable quantum particles follows either Fermi-Dirac statistics for particles with half-integer spin (fermions) or Bose-Einstein statistics for particles with integer spin (bosons).
- For example, consider a system of non-interacting fermions, such as electrons in a metal. Due to their indistinguishability, the Pauli exclusion principle restricts the occupation of quantum states by electrons.

- Distinguishable particles are unique entities with distinct properties, while non-distinguishable particles are identical and indistinguishable.
- The distribution of distinguishable particles follows classical or quantum statistics depending on the context, while the distribution of non-distinguishable particles follows quantum statistics.
- Quantum statistics account for the indistinguishability of particles and lead to phenomena such as Bose-Einstein condensation and Fermi-Dirac degeneracy.

## **Maxwell-Boltzmann statistics**

Maxwell-Boltzmann statistics describe the distribution of particles in an ideal gas at thermal equilibrium. The derivation of Maxwell-Boltzmann statistics involves determining the probability distribution function for the velocities of gas particles, assuming that the gas particles are non-interacting and follow classical mechanics. Here's a simplified derivation:

### Assumptions:

- The gas consists of a large number of identical particles (atoms or molecules) that do not interact with each other except through elastic collisions.
- The gas is in thermal equilibrium at temperature  $T$ .
- The gas is in a container of fixed volume  $V$ .
- Gas particles are non-interacting.
- Gas particles follow classical mechanics.
- Gas particles are indistinguishable.

### Derivation:

- Partitioning Phase Space:** Consider a gas of  $N$  identical particles confined in a volume  $V$ . The phase space for a single particle is six-dimensional (three for position and three for momentum).
- Counting States:** We partition the phase space into small volume elements  $\Delta x \Delta y \Delta z$  and  $\Delta p_x \Delta p_y \Delta p_z$ . The number of states within a volume element in phase space is given by  $\Delta x \Delta y \Delta z \Delta p_x \Delta p_y \Delta p_z$ .
- Determination of Phase Space Volume:** The volume of a region in phase space,  $\Delta \Gamma$ , is given by the product of the volume elements:  $\Delta \Gamma = \Delta x \Delta y \Delta z \Delta p_x \Delta p_y \Delta p_z$



4. **Occupation of States:** The probability that a particle occupies a state within a volume element  $\Delta\Gamma\Delta\Gamma$  is proportional to  $\Delta\Gamma\Delta\Gamma$ .

5. **Velocity Distribution:** We're interested in the distribution of velocities. The velocity of a particle is related to its momentum:  $p=mv\Rightarrow\Delta p=m\Delta v$  The velocity space volume element  $\Delta v_x\Delta v_y\Delta v_z$  is related to the momentum space volume element  $\Delta p_x\Delta p_y\Delta p_z$  by  $\Delta v_x\Delta v_y\Delta v_z = (\Delta p_x\Delta p_y\Delta p_z)/m^3$ .

6. **Determining the Distribution:** The number of states within a velocity space volume element  $\Delta v_x\Delta v_y\Delta v_z$  is given by  $\Delta v_x\Delta v_y\Delta v_z/m^3$ .

7. **Maxwell-Boltzmann Distribution:** The probability distribution function  $f(v_x, v_y, v_z)$  for the velocity components  $v_x, v_y, v_z$  is proportional to the number of states in the corresponding velocity space volume element. This leads to the Maxwell-Boltzmann distribution:  $f(v_x, v_y, v_z) \propto e^{-2kTmv^2}$  Where  $T$  is the temperature and  $k$  is the Boltzmann constant.

8. **Normalization:** To ensure that the probability distribution function is properly normalized, one must integrate it over all velocities and divide by the normalization constant.

The Maxwell-Boltzmann distribution provides a probability distribution for the velocities of gas particles in an ideal gas at thermal equilibrium. It describes the likelihood of finding particles with different velocities and is essential for understanding the behavior of gases in classical thermodynamics.

#### Derivation:

1. **Energy Levels:**

- In classical mechanics, the kinetic energy of a particle with mass  $m$  and velocity  $v$  is given by  $E = \frac{1}{2}mv^2$ .
- For a gas in three dimensions, the kinetic energy can be expressed in terms of the velocity components along each axis.

## 2. Density of States:

- The number of states (microstates) available to a particle with energy between  $E$  and  $E+dE$  is proportional to  $E^{3/2}dE$ . This is derived from the volume of the shell in velocity space.
- The density of states function  $g(E)$  describes the number of states per unit energy interval.

## 3. Boltzmann Distribution:

- According to the Boltzmann distribution, the probability  $P(E)$  of finding a particle in a state with energy  $E$  is proportional to  $e^{-\beta E}$ , where  $\beta = 1/kT$  and  $k$  is the Boltzmann constant.
- Combining the density of states  $g(E)$  with the Boltzmann distribution, we obtain the probability density function for the energy levels.

## 4. Maxwell-Boltzmann Distribution:

- By converting the probability density function from energy space to velocity space using the relation between energy and velocity, we derive the Maxwell-Boltzmann distribution function for the speeds of particles.

## 5. Normalization:

- The distribution function is then normalized to ensure that the total probability of finding a particle with any velocity is equal to 1.
- The final expression for the Maxwell-Boltzmann distribution function is obtained, which describes the probability density of finding a particle with a given speed  $v$  in the gas at temperature  $T$ .

The Maxwell-Boltzmann distribution arises from statistical mechanics principles and provides a probabilistic description of the speeds of particles in a gas at thermal equilibrium. It is a fundamental concept in understanding the behavior of gases and plays a key role in various applications in physics, chemistry, and engineering.

### **Bose-Einstein statistics**

The Bose-Einstein statistics describe the distribution of indistinguishable particles, which can occupy the same quantum state. It applies to particles with integer spin, such as bosons. The derivation involves considering the statistical mechanics of particles in a system obeying the Bose-Einstein distribution. Here's a simplified derivation:

#### **Assumptions:**

1. We consider a system of non-interacting particles.
2. The particles are indistinguishable, meaning there is no way to tell them apart.

#### **Derivation:**

1. **Partition Function ( $Z$ ):** The partition function for a system of non-interacting particles is given by: all states  $e^{-\beta E_i}$  where  $E_i$  is the energy of state  $i$  and  $\beta = kT^{-1}$  where  $k$  is the Boltzmann constant and  $T$  is the temperature.
2. **Occupation Number:** The probability  $P_i$  of a state  $i$  being occupied is given by:

$$P_i = \frac{e^{-\beta E_i}}{Z}$$

3. **Total Number of Particles ( $N$ ):** The total number of particles  $N$  is given by the sum of the number of particles in each state  $n_i$  weighted by the probability of occupation
4.  $N = \sum n_i P_i$

5. **Energy  $E$  and Chemical Potential ( $\mu$ ):** We define the energy  $E$  as:  $E = \sum niE_i$  and the chemical potential  $\mu = -\beta^{-1} \ln(NZ)$
6. **Bose-Einstein Distribution:** From the above expressions, we obtain the Bose-Einstein distribution by substituting  $P_i$  and  $\mu$  into the expression for  $ni$ . This gives the average number of particles in state  $i$  as  $n_i = \frac{1}{e^{\beta(E_i - \mu)} - 1}$

The Bose-Einstein distribution function is a probability distribution used in statistical mechanics to describe the distribution of particles over various energy states in a system. It is named after Satyendra Nath Bose and Albert Einstein, who first proposed its use.

The expression for the Bose-Einstein distribution function  $f(E)$  is given by:

$$f(E) = \frac{1}{e^{(E-\mu)/k_B T} - 1}$$

Where:

- $E$  is the energy of the state,
- $\mu$  is the chemical potential of the system,
- $k_B$  is the Boltzmann constant,
- $T$  is the temperature of the system.

This distribution function describes the average number of particles occupying a particular energy state in a system governed by Bose-Einstein statistics.

This expression represents the Bose-Einstein distribution, which governs the probability of finding a particle in a given energy state  $E_i$  for a system obeying Bose-Einstein statistics. It shows that unlike in classical statistics (where the denominator is  $e^{\beta(E_i - \mu)} + 1$ ), there is no restriction on the occupation numbers, allowing for the possibility of multiple particles occupying the same quantum state.

## **Fermi-Dirac statistics**

Fermi-Dirac statistics is a branch of quantum statistics that describes the behavior of particles known as fermions, which obey the Pauli exclusion principle. It is named after Enrico Fermi and Paul Dirac, who developed the statistical framework for understanding the distribution of fermions in a system. Fermi-Dirac statistics plays a crucial role in understanding the behavior of electrons in solids, such as in metals and semiconductors, as well as in nuclear physics and astrophysics.

### **Introduction:**

Fermi-Dirac statistics deals with systems of indistinguishable fermions, particles with half-integer spin (e.g., electrons, protons, neutrons). Unlike bosons, fermions cannot occupy the same quantum state simultaneously due to the Pauli exclusion principle. Therefore, understanding the distribution of fermions in various energy levels under different conditions, such as temperature and chemical potential, is essential for describing the behavior of fermionic systems.

The Fermi-Dirac statistics describe the statistical behavior of particles with half-integer spin, such as fermions. These particles obey the Pauli exclusion principle, which states that no two fermions can occupy the same quantum state simultaneously. The Fermi-Dirac distribution function gives the probability of finding a fermion in a particular quantum state at thermal equilibrium. Here's a simplified derivation:

### **Assumptions:**

1. **Particles are indistinguishable:** Like in Bose-Einstein statistics, the particles are considered indistinguishable. This means that exchanging any two particles results in the same physical state of the system.
2. **Pauli Exclusion Principle:** Fermions obey the Pauli exclusion principle, which states that no two fermions can occupy the same quantum state simultaneously. This principle plays a crucial role in determining the occupation of energy states in fermionic systems.
3. **Occupation Probability:** The occupation probability  $f(E)$  of a single-particle energy level  $E$  is defined as the probability of finding a fermion in that energy state. Unlike bosons, where the occupation probability can exceed unity, for fermions, the occupation probability is limited to either 0 or 1 due to the Pauli exclusion principle.
4. The system is in contact with a heat reservoir at temperature  $T$ .

#### Derivation:

#### 1. Single-Particle States:

- Consider a system of non-interacting fermions in a box potential. Each fermion can occupy a single-particle state described by the quantum numbers  $n_x, n_y, n_z$  for a 3D box or  $n$  for a 1D box.

#### 2. Occupation Numbers:

- The number of fermions occupying a single-particle state is either 0 or 1 due to the Pauli exclusion principle. We define the occupation number  $n_i$  for state  $i$  as:  

$$n_i = \begin{cases} 1 & \text{if state } i \text{ is occupied} \\ 0 & \text{if state } i \text{ is unoccupied} \end{cases}$$

#### 3. Fermi-Dirac Distribution:

- The probability  $f(E_i)$  of finding a fermion in a state with energy  $E_i$  is given by the Fermi-Dirac distribution function:  

$$f(E_i) = \frac{1}{e^{\beta(E_i - \mu)} + 1}$$
- Here,  $\beta = 1/kT$  is the inverse temperature,  $k$  is the Boltzmann constant, and  $\mu$  is the chemical potential.

#### 4. Chemical Potential:

- The chemical potential  $\mu$  is determined by the condition that the average number of fermions is fixed. This condition leads to the relation:  $\langle N \rangle = \sum_i f(E_i)$

#### 5. Normalization:

- The Fermi-Dirac distribution function is normalized to ensure that the total probability of finding a fermion in any state is equal to the total number of fermions in the system.
- The final expression for the Fermi-Dirac distribution function  $f(E_i)$  is obtained, which describes the probability of finding a fermion in a state with energy  $E_i$  at temperature  $T$  and chemical potential  $\mu$ .

The Fermi-Dirac distribution function arises from the statistical mechanics of fermions and incorporates the Pauli exclusion principle. It provides a probabilistic description of the occupation of single-particle states by fermions in a system at thermal equilibrium. The distribution function is fundamental in understanding the behavior of fermionic systems, such as electrons in metals and degenerate gases.

### Partition Function

In statistical mechanics, the partition function ( $Z$ ) is a fundamental concept used to describe the statistical properties of a system in thermodynamic equilibrium. It encapsulates all the information about the system's microstates, including their energies and degeneracies, and allows for the calculation of various thermodynamic quantities. The partition function is defined differently for different ensembles (e.g., microcanonical, canonical, grand canonical), but its basic purpose remains the same: to provide a bridge between the microscopic properties of a system and its macroscopic thermodynamic behavior.

### Microcanonical Ensemble:

In the microcanonical ensemble, the partition function is defined as the sum over all microstates ( $i$ ) accessible to the system, weighted by the Boltzmann factor ( $e^{-\beta E_i}$ ):

$$Z = \sum_i e^{-\beta E_i}$$

Where:

- $E_i$  is the energy of microstate  $i$ ,
- $\beta = 1/kT$  is the inverse temperature (where  $k$  is the Boltzmann constant and  $T$  is the temperature).

### Canonical Ensemble:

In the canonical ensemble, where the system is in thermal equilibrium with a heat reservoir at constant temperature  $T$ , the partition function is given by:

$$Z = \sum_i e^{-\beta E_i}$$

However, in this case, the sum is taken only over those states that have the same total energy as the system.

### Grand Canonical Ensemble:

In the grand canonical ensemble, where the system is allowed to exchange both energy and particles with a reservoir at constant temperature  $T$  and chemical potential  $\mu$ , the partition function is:

$$Z = \sum_i e^{-\beta(E_i - \mu N_i)}$$

Where  $N_i$  is the number of particles in microstate  $i$ .

**Uses:**



- Once the partition function is known, various thermodynamic quantities such as the Helmholtz free energy, entropy, internal energy, and average values of observables can be derived using appropriate mathematical manipulations.
- The partition function serves as a central quantity in statistical mechanics, providing a framework for connecting microscopic properties of a system to macroscopic observables.

The partition function is a crucial concept in statistical mechanics, allowing for the calculation of thermodynamic properties of a system from its microscopic state. It provides a powerful tool for understanding the behavior of complex systems in equilibrium and is widely used in theoretical physics, chemistry, and materials science.

The electronic partition function (electronic~~electronic~~) represents the contribution of electronic energy levels to the overall partition function of a molecule. It is given by summing over all electronic states of the molecule, weighted by their respective degeneracies and Boltzmann factors.

### **Translational Partition function**

The translational partition function, often denoted as  $Q_{\text{trans}}$ , represents the contribution of the translational degrees of freedom to the overall partition function of a system. It quantifies the distribution of particles in momentum space and is crucial in statistical mechanics for calculating various thermodynamic properties.

The expression for the translational partition function depends on the system's dimensionality (whether it's a monoatomic gas, diatomic gas, or a solid) and whether the particles are classical or quantum. Here are the expressions for different cases:

#### **Monoatomic Gas:**

For a monoatomic gas of  $N$  identical particles confined to a volume  $V$  at temperature  $T$  in three dimensions, the translational partition function is given by the expression:

$$Q_{\text{trans}} = V^N / N! (2\pi m k_B T / h^2)^{3N/2}$$

Where:

- $V$  is the volume,
- $N$  is the number of particles,
- $m$  is the mass of a single particle,
- $k_B$  is the Boltzmann constant,
- $T$  is the temperature,
- $h$  is the Planck constant.

### **Diatomic Gas:**

For diatomic molecules, the expression differs slightly because of the additional rotational degrees of freedom. The expression includes a factor of  $(Ik_B T / \sigma^2)^{3/2}$ , where  $I$  is the moment of inertia and  $\sigma$  is the symmetry number.

### **Solid:**

For a solid, where the particles are confined to a crystal lattice, the expression is different. The translational partition function for a solid is typically related to the Debye model for the density of states, which considers the phonon modes in the solid.

### **Quantum Effects:**

In the case of quantum particles (e.g., electrons in a metal), the expression for the translational partition function may involve quantum statistics and may not directly correspond to the classical expression.

These expressions provide a way to calculate the contribution of translational degrees of freedom to the overall thermodynamic properties of a system.

### Expression for electronic $q_{\text{electronic}}$ :

$$q_{\text{electronic}} = \sum_{\text{electronic states}} g_i e^{-\beta E_i}$$

Where:

- $g_i$  is the degeneracy of the  $i$ th electronic state.
- $E_i$  is the energy of the  $i$ th electronic state.
- $\beta = 1/kT$  is the inverse temperature, where  $k$  is the Boltzmann constant and  $T$  is the temperature.

### Derivation:

#### 1. Electronic Energy Levels:

- A molecule has various electronic energy levels, each corresponding to different electronic configurations.
- These energy levels are typically determined from quantum mechanical calculations or experimental spectroscopic data.

#### 2. Degeneracy ( $g_i$ ):

- The degeneracy of an electronic state ( $g_i$ ) is the number of microstates corresponding to that energy level.
- It accounts for the number of different ways the system can achieve the same energy.

#### 3. Boltzmann Factor:

- The Boltzmann factor  $e^{-\beta E_i}$  represents the probability of finding the system in the  $i$ th electronic state at temperature  $T$ .

- It weighs the contribution of each electronic state to the partition function based on its energy.

#### 4. **Summation Over Electronic States:**

- The electronic partition function is obtained by summing over all electronic states of the molecule.
- Each term in the sum represents the contribution of a specific electronic state to the overall partition function.

#### 5. **Normalization:**

- The electronic partition function is typically normalized to ensure that the total probability of finding the molecule in any electronic state is equal to 1.

#### **Example:**

For a diatomic molecule like  $O_2$ , the electronic partition function would involve summing over the electronic states corresponding to its ground state, excited states, and possibly dissociative states. Each electronic state would have its energy ( $E_i$ ) and degeneracy ( $g_i$ ), contributing to the overall electronic partition function.

The electronic partition function provides a statistical description of the electronic energy levels of a molecule at a given temperature. It is a key quantity in molecular spectroscopy and thermodynamics, allowing for the calculation of thermodynamic properties and interpretation of experimental data.

#### **Rotational partition function for monoatomic Gas:**

For a monoatomic gas, there's only translational motion available, and no rotational or vibrational degrees of freedom. Hence, the partition function for rotation is trivially equal to 1.

$$Q_{\text{rot, monoatomic}} = 1$$

### Diatomic Gas:

For a diatomic molecule, the rotational partition function depends on the moment of inertia  $I$  and the temperature  $T$ . The rotational energy levels are quantized according to  $E_J = J(J+1) \frac{h^2}{2I}$ , where  $J$  is the rotational quantum number and  $h$  is the reduced Planck constant.

The partition function  $Q_{\text{rot, diatomic}}$  is given by the sum over all possible rotational states:

$$Q_{\text{rot, diatomic}} = \sum_{J=0}^{\infty} (2J+1) e^{-J(J+1)\theta_r/T}$$

Where  $\theta_r = \frac{h^2}{2Ik_B}$  is the characteristic rotational temperature, and  $k_B$  is the Boltzmann constant.

### 3. Polyatomic Gas:

For a polyatomic molecule with  $n$  atoms, the rotational partition function becomes more complex due to the presence of multiple rotational axes. The total rotational partition function  $Q_{\text{rot, polyatomic}}$  can be expressed as the product of rotational partition functions along each principal axis:

$$Q_{\text{rot, polyatomic}} = Q_{\text{rot,1}} \times Q_{\text{rot,2}} \times Q_{\text{rot,3}}$$

Where  $Q_{\text{rot, } i}$  is the rotational partition function associated with the  $i$ -th rotational axis. The moment of inertia  $I_i$  for each axis can be calculated based on the molecule's geometry.

### Derivation Details:

To derive the expression for rot, diatomic  $Q_{\text{rot, diatomic}}$ , we consider the rotational energy levels of a diatomic molecule. By Boltzmann statistics, the probability  $p_J$  of a molecule being in the  $J$ -th rotational state is given by:

$$p_J = Z_{\text{rot}}^{-1} e^{-J(J+1)/T} / \theta_r$$

Where  $Z_{\text{rot}}$  is the rotational partition function, and  $\theta_r$  is the characteristic rotational temperature.

The partition function  $Z_{\text{rot}}$  is then obtained by summing over all possible rotational states  $J$ :

$$Z_{\text{rot}} = \sum_{J=0}^{\infty} e^{-J(J+1)/T} / \theta_r$$

This sum represents the contribution of rotational degrees of freedom to the overall partition function of the system. Similar derivations can be made for polyatomic molecules, but considering the moments of inertia along each axis.

### **The equipartition theorem**

The equipartition theorem is a principle in statistical mechanics that relates the energy of a system to its temperature. It states that in thermal equilibrium, each quadratic term in the total energy of a system has an average energy of  $kT/2$ , where  $k$  is the Boltzmann constant and  $T$  is the temperature of the system measured in kelvin.

This theorem is particularly useful in understanding the distribution of energy among different degrees of freedom in a system. For example, in a classical system, each quadratic term in the Hamiltonian (representing kinetic or potential energy) contributes  $kT/2$  to the average total energy per degree of freedom, assuming the system is in thermal equilibrium.

The equipartition theorem has important applications in various fields of physics, including classical mechanics, thermodynamics, and quantum mechanics. However, it's important to note that the theorem has limitations and may not always hold true, especially in systems where quantum effects or interactions between particles become significant.

The expressions for free energy, enthalpy, and entropy in terms of the partition function depend on the specific thermodynamic system you're considering. However, I can provide you with general expressions for these quantities in terms of the partition function.

1. **Free Energy (G):** The Helmholtz free energy, denoted by  $G$ , is defined as:

$$G = -kT \ln Q$$

where  $k$  is the Boltzmann constant,  $T$  is the temperature, and  $Q$  is the partition function of the system.

2. **Enthalpy (H):** The enthalpy, denoted by  $H$ , is related to the free energy through:

$$H = G + TS$$

where  $S$  is the entropy of the system.

3. **Entropy (S):** The entropy, denoted by  $S$ , is given by:

$$S = - \left( \frac{\partial G}{\partial T} \right)_{P,N}$$

where  $P$  is the pressure and  $N$  is the number of particles.

To express these quantities in terms of the partition function, you typically need to calculate derivatives of the partition function with respect to temperature or other relevant variables. For example, to find the entropy, you'd take the derivative of  $G$  with respect to temperature. This involves applying the chain rule and manipulating the expression accordingly.

These expressions provide a convenient way to relate thermodynamic quantities to the statistical properties of the system described by the partition function. However, the actual calculations may involve some mathematical manipulation and possibly numerical methods, depending on the complexity of the system.

1. **Residual Entropy:** Residual entropy refers to the entropy that remains in a system even at absolute zero temperature. It arises from degenerate ground states, where multiple microstates have the same energy. The residual entropy  $S_{\text{res}}$  is related to the number of degenerate ground states  $\Omega_0$  by

$$S_{\text{res}} = k \ln \Omega_0$$

where  $k$  is the Boltzmann constant.

2. **Internal Energy:** The internal energy  $U$  of a system can be expressed in terms of the partition function  $Q$  as:



$$U = -\partial/\beta \partial \ln Q$$

where  $\beta = 1/kT$  is the reciprocal of the temperature times Boltzmann's constant.

3. **Helmholtz Free Energy:** The Helmholtz free energy  $A$  is related to the partition function  $Q$

$$A = -kT \ln Q$$

These expressions provide a statistical mechanics perspective on these thermodynamic properties, connecting them to the underlying microstates of the system via the partition function. The partition function encapsulates information about the system's energy levels and their degeneracies, allowing us to derive various thermodynamic properties.

These expressions provide a direct connection between thermodynamic properties and the statistical properties of the system encoded in its partition function. They allow us to analyze the behavior of the system at equilibrium and understand its thermodynamic properties in terms of its microscopic states.

### Heat capacity of a gas

The heat capacity of a monoatomic ideal gas and a diatomic ideal gas can be expressed in terms of the Boltzmann constant  $k$  and the molar mass  $M$  of the gas molecules.

1. **Monoatomic Ideal Gas:** For a monoatomic ideal gas, each molecule has three degrees of freedom associated with translational motion. The molar heat capacity at constant volume ( $C_V$ ) and at constant pressure ( $C_P$ ) for a monoatomic ideal gas are

related as follows:  $C_P = C_V + R$  where  $R$  is the gas constant ( $R = kN_A$ , where  $N_A$  is Avogadro's number).

The molar heat capacity at constant volume  $C_V$  for a monoatomic ideal gas is given by:  $C_V = 3/2R$

And the molar heat capacity at constant pressure  $C_P$  is:  $C_P = 5/2R$

2. **Diatomic Ideal Gas:** For a diatomic ideal gas, each molecule has additional degrees of freedom associated with rotational motion in addition to translational motion. At room temperature, diatomic molecules generally contribute 5 degrees of freedom: 3 translational and 2 rotational. Therefore, for a diatomic ideal gas, the molar heat capacity at constant volume  $C_V = 7/2R$

And the molar heat capacity at constant pressure  $C_P$  is:  $C_P = 9/2R$

The additional  $1/2R$  contribution in  $C_V$  and  $C_P$  for diatomic gases compared to monoatomic gases arises from the extra rotational degrees of freedom.

These expressions are valid for ideal gases under conditions where quantum effects are negligible, such as at high temperatures or low pressures.

Ortho- and para-hydrogen are different nuclear spin isomers of the hydrogen molecule. They have different energy levels due to the different spins of their hydrogen nuclei. As a result, they have slightly different heat capacities.

1. **Orthohydrogen:** Orthohydrogen has nuclear spins aligned parallel to each other, resulting in higher energy levels. At room temperature, the rotational energy levels of orthohydrogen are populated to a greater extent compared to parahydrogen. Therefore, it has a higher heat capacity.
2. **Parahydrogen:** Parahydrogen has nuclear spins aligned antiparallel to each other, resulting in lower energy levels. At room temperature, the rotational energy levels of

parahydrogen are less populated compared to orthohydrogen. Therefore, it has a lower heat capacity.

Exact expressions for the heat capacities of ortho- and parahydrogen can be quite complex and are typically derived from statistical mechanics using partition functions and considering the different energy levels associated with their rotational states. The heat capacities of ortho- and parahydrogen can also vary with temperature.

As a reference, at low temperatures, the heat capacity of parahydrogen tends to approach that of a monoatomic gas, while orthohydrogen behaves more like a diatomic gas. However, at higher temperatures, both ortho- and parahydrogen approach the heat capacity of a diatomic gas due to increased population of higher energy rotational states.

The heat capacities of ortho- and parahydrogen gases can be expressed in terms of their rotational degrees of freedom and statistical mechanics.

For hydrogen gas, the rotational heat capacity can be calculated using the following expressions:

1. **Rotational heat capacity at constant volume  $C_V$ :**  $C_V = 2R + 2R = 4R$
2. **Rotational heat capacity at constant pressure  $C_P$  for orthohydrogen:**
3.  $C_P = C_V + R = 4R + R = 5R$
4. **Rotational heat capacity at constant pressure  $C_P$  for parahydrogen:**  $C_P = C_V + R/2 = 4R + R/2 = 4.5R$

Where:

- $R$  is the gas constant.

- The factor  $1/2R$  represents the contribution of each rotational degree of freedom. Hydrogen has two rotational degrees of freedom per molecule due to its diatomic nature.
- For orthohydrogen, both rotational states are populated at room temperature, so it behaves like a diatomic molecule, resulting in a heat capacity of  $1/2R$ .
- For parahydrogen, only one of the two rotational states is populated at room temperature, hence it behaves more like a monoatomic gas, leading to a lower heat capacity of  $3/2R$ .

These expressions provide a simplified model for the heat capacities of ortho- and parahydrogen gases based on their rotational degrees of freedom.

### Heat capacity of solids

The heat capacity of a solid can be described using the Debye model or the Einstein model, both of which provide approximations for the heat capacity of solids at low temperatures.

1. **Debye Model:** The Debye model assumes that the solid consists of a lattice of atoms vibrating as phonons. The heat capacity  $C_V$  of a solid at constant volume according to the Debye model is given by:

$$C_V = 9Nk(T/\Theta_D)^3 \int_0^{\Theta_D/T} \left[ \frac{4}{x^2} - \frac{1}{(x^2-1)^2} \right] dx$$

where:

- $N$  is the number of atoms in the solid,
- $k$  is the Boltzmann constant,
- $T$  is the temperature,
- $\Theta_D$  is the Debye temperature.

The Debye temperature  $D$  is a characteristic temperature for the solid and is related to its elastic properties.

The Debye model is a theoretical model used to describe the heat capacity of solids, especially at low temperatures. It assumes that the atoms in the solid vibrate as phonons, which are collective excitations of the atomic lattice. Here's a breakdown of its temperature dependence and its merits and demerits:

**Temperature Dependence:** The Debye model predicts the following temperature dependence of the heat capacity ( $C_V$ ) of a solid:

1. At low temperatures:

- The heat capacity varies with temperature cubically:  $C_V \propto T^3$ .
- This behavior is known as the Debye  $T^3$  law.
- At low temperatures, the heat capacity approaches zero, as the thermal energy is insufficient to excite higher vibrational modes in the solid.

2. At high temperatures:

- The heat capacity approaches a constant value.
- At high temperatures, all vibrational modes are excited, and the heat capacity becomes independent of temperature.
- This behavior is consistent with the Dulong-Petit law, which states that the molar heat capacity of a solid at constant volume is approximately 3 times the gas constant  $R$ .

**Merits:**

1. **Predictive Power:** The Debye model provides a reasonable approximation for the heat capacity of solids over a wide range of temperatures, from absolute zero up to temperatures where classical thermodynamics holds.

2. **Incorporates Collective Behavior:** It incorporates the collective behavior of atoms in a solid through phonons, which makes it a more realistic model than some simpler models.
3. **Relatively Simple:** While it's more complex than the Einstein model, the Debye model is still relatively simple compared to more sophisticated models, making it tractable for calculations.

#### Demerits:

1. **Low Temperature Limit:** The Debye model fails to accurately predict the behavior of heat capacity at very low temperatures. Experimentally, heat capacities do not tend to zero at absolute zero, as predicted by the Debye model.
2. **Crystal Symmetry:** It assumes isotropic and homogeneous behavior of the solid, which may not hold true for all materials with complex crystal structures.
3. **Specific Heat Ratios:** In some cases, the Debye model may not accurately predict the specific heat ratios of different materials due to variations in their atomic structures.

Despite these limitations, the Debye model remains a valuable tool for understanding the behavior of heat capacity in solids and is widely used in theoretical and experimental studies of condensed matter physics.

#### Einstein model

In the Einstein model of solids, the variation of temperature ( $T$ ) affects the heat capacity ( $CV$ ) of the solid. The Einstein model describes a solid as a collection of independent harmonic oscillators, each with the same frequency  $\omega_E$ , known as the Einstein frequency. The heat capacity at constant volume  $CV$  for the Einstein model is given by:

$$C_V = 3Nk \left( \frac{\omega E}{kT} \right)^2 \frac{e^{-\omega E/kT}}{(e^{-\omega E/kT} - 1)^2}$$

In this expression:

- $N$  is the number of oscillators (number of atoms in the solid).
- $k$  is the Boltzmann constant.
- $\hbar$  is the reduced Planck constant.
- $\omega E$  is the Einstein frequency.
- $T$  is the temperature.

As the temperature  $T$  varies, the term  $\frac{\omega E}{kT}$  in the equation also changes. When  $T$  is much smaller than  $\frac{\omega E}{k}$ , the exponential term  $e^{-\omega E/kT}$  becomes large and dominates the heat capacity. In this limit, the heat capacity approaches a constant value:

$$C_V \approx 3Nk \left( \frac{\omega E}{kT} \right)^2$$

On the other hand, when  $T$  is much larger than  $\frac{\omega E}{k}$ , the exponential term  $e^{-\omega E/kT}$  approaches 1, and the heat capacity approaches the classical limit:

$$C_V \approx 3Nk$$

This behavior illustrates the limitations of the Einstein model at both low and high temperatures. At low temperatures, the Einstein model predicts that the heat capacity approaches zero, which is not observed experimentally. At high temperatures, the Einstein model predicts that the heat capacity does not vary with temperature, which contradicts the Dulong-Petit law.

## Unit-3

### Irreversible Thermodynamics

In classical thermodynamics, we have seen time dependent variation of thermodynamic quantities such as internal energy (U), enthalpy (H), entropy (S), Gibbs free energy (G) etc. are not considered. Classical thermodynamics deals with transitions from one equilibrium state to another brought about by different mechanical or chemical methods. Non equilibrium thermodynamics is that branch of thermodynamics that deals with the system which are not in thermodynamic equilibrium. But such systems can be described by non-equilibrium state variables which represent an extrapolation of variables used to specify system in thermodynamic equilibrium.

All the natural processes occurring are not in thermodynamic equilibrium or irreversible in nature. Systematic macroscopic and general thermodynamics of irreversible process are obtained from Onsager theorem. Irreversible thermodynamics essentially deals with qualitative and quantitative changes occurring with respect to time. Many physiochemical processes which are typically known as irreversible process include conduction of heat, diffusion of matter and chemical reactions. Irreversible thermodynamics is a branch of thermodynamics that deals with processes that do not occur in a state of equilibrium. Unlike reversible processes, which can be theoretically reversed without leaving any trace on the system or its surroundings, irreversible processes involve dissipative effects such as friction, heat conduction, viscosity, and chemical reactions, leading to a net increase in entropy.

Irreversible thermodynamics provides a framework for analyzing and understanding such processes, including their underlying principles and governing equations. It



focuses on the macroscopic behavior of systems undergoing irreversible changes, often using concepts such as entropy production and Onsager's reciprocal relations.

Here's a brief overview of some key concepts in irreversible thermodynamics:

The difference between equilibrium and non-equilibrium thermodynamics

One basic difference between equilibrium and non-equilibrium thermodynamics lies in the behaviour of inhomogeneous systems which require knowledge of rate of reaction but this is not considered in equilibrium thermodynamics of homogeneous systems.

Time courses of physical processes are ignored by equilibrium thermodynamics but irreversible thermodynamics explain the time courses of physical processes in continuous detail. Consequently, equilibrium thermodynamics permits those processes that pass through states far from thermodynamic equilibrium that cannot be described even by variables admitted for non-equilibrium thermodynamics like time rate of change of temperature and pressure.

Equilibrium thermodynamics use the concept of quasi-static process. A quasi-static process is conceptually (timeless and physically impossible) mathematical passage along continuous path of states of thermodynamic equilibrium. But this concept of quasi-static process is not used by non-equilibrium thermodynamics.

Non-equilibrium thermodynamics states that continuous time-courses, need its state variables to have a very close connection with those of equilibrium thermodynamics

1. **Entropy Production:** In irreversible processes, entropy tends to increase due to the dissipation of energy. Entropy production quantifies this increase and serves as a measure of irreversibility in a system. It is typically expressed as the rate of change of entropy with respect to time.

2. **Onsager's Reciprocal Relations:** Onsager's reciprocal relations provide a mathematical framework for describing the relationships between fluxes and forces in a system undergoing irreversible processes. These relations establish symmetry properties between pairs of conjugate fluxes and forces, facilitating the analysis of transport phenomena such as heat conduction, diffusion, and electrical conduction.
3. **Nonequilibrium Thermodynamics:** Nonequilibrium thermodynamics extends the principles of equilibrium thermodynamics to systems far from thermodynamic equilibrium. It provides a systematic approach for analyzing and predicting the behavior of systems undergoing irreversible changes, including the development of constitutive equations and transport coefficients.
4. **Linear Response Theory:** Linear response theory is a powerful tool in irreversible thermodynamics for studying the behavior of systems in the presence of small perturbations. It allows for the calculation of linear response coefficients, which describe how a system responds to external perturbations, such as changes in temperature, pressure, or concentration.

Irreversible thermodynamics finds applications in various fields, including engineering, physics, chemistry, and biology, where processes involving heat transfer, fluid flow, chemical reactions, and biological transport are common. Understanding irreversible processes is essential for designing efficient energy conversion systems, optimizing chemical processes, and modeling complex biological systems.

In the context of irreversible thermodynamics, the conservation of mass and energy in an open system is described by balance equations that account for the flow of mass and energy across the system boundaries. These balance equations are fundamental in analyzing processes such as fluid flow, heat transfer, and chemical reactions occurring in open systems. Two key theories are often used to describe these conservation principles:

The total entropy change  $dS$  of a system can be expressed as the sum of the entropy change arising from system ( $d_{in}S$ ) and its interaction with surroundings ( $d_{ex}S$ )

$$dS_{total} = d_{ex}S + d_{in}S$$

where,

$d_{ex}S$  = entropy change due to surroundings (external system)

$d_{in}S$  = entropy change within system (internal system)

$dS_{total}$  = Total entropy

Entropy change within system can be equal to or greater than zero.

$d_{in}S=0$  in reversible system(or equilibrium)

$d_{in}S > 0$  in irreversible process(non-equilibrium)

If  $d_{ex}S=0$  (adiabatic transformation) then  $dS_{total}=d_{in}S \geq 0$

There is no restriction on the sign of  $d_{ex}S$ , but  $d_{in}S$  should always be positive (irreversible thermodynamics).

The quantity  $Td_{in}S$  is called the uncompensated heat by Clausius.

The local entropy production  $\sigma$  is defined as the sum of product of fluxes and conjugate forces. The entropy production could always be isolated for any process. It is also equal to or greater than zero i.e.

$$\sigma \geq 0$$

For the reversible process, entropy production is equal to zero. The dissipation factor 'Y' is defined as  $\frac{dQ}{T}$  (where T is absolute temperature). Y is positive dissipation as it is natural consequence of irreversible process.  $\sigma$  can

also be represented as  $\frac{dQ}{T}$  /

Onsager's formalism of irreversible thermodynamics states that "the entropy production vis-a-vis dissipation function can be represented as sum of fluxes and their conjugate forces".

Systems exhibiting non-equilibrium process are much more complex and they undergo fluctuations of more extensive quantities. Some boundary conditions which are imposed on them particularly intensive variables like temperature gradient or distorted collective motions are called thermodynamics forces. Now, discussing different laws of thermodynamics.

### **Zeroth law of thermodynamics**

Zeroth-law of thermodynamics states that "if two bodies A and B having different temperature when come in contact with each other they both attain same temperature. In such system mass won't get exchanged but energy is exchanged. Thermometer is based on Zeroth Law.

### **First law of thermodynamics**

The first law of thermodynamics is also known as law of conservation of energy i.e. energy can neither be created nor be destroyed.

This law states that if system absorbs heat from the surroundings, internal energy of the system increases. This rise in internal energy can be given back to surroundings in the form of work.

Mathematical form of first law is:-

$$q = \Delta U + w$$

Where  $\Delta U$  is change in internal energy,  $q$  is the heat absorbed,  $w$  is the work done.

We also know that work done is given by

$$w = P\Delta V$$

Substituting this in equation , we get

$$q = \Delta U + P\Delta V$$

Now the heat absorbed keeping the pressure of the system constant will be given by,

$$q = (U_2 - U_1) + P(V_2 - V_1)$$

$$q_p = (U_2 + PV_2) - (U_1 + PV_1)$$

In the above equation  $U$  denotes the internal energy,  $P$  is pressure and  $V$  is the volume. All three  $U$ ,  $P$  and  $V$  are state functions the quantity  $U + PV$  should also be state function.

The quantity  $U + PV = H$  is known as enthalpy and change in enthalpy will give amount of heat absorbed at constant pressure i.e.

$$q_p = H_2 - H_1$$

Where  $H_1$  is initial enthalpy and  $H_2$  is the final enthalpy of the system. Then the equation can be written as

$$q_p = \Delta H$$

where H is heat absorbed by system at constant pressure.

### Second law of thermodynamics

The second law of thermodynamics forms the most important law in classical thermodynamics from which the criteria of spontaneity and equilibrium of a system are derived. From this law it can be deduced that at equilibrium, entropy of an isolated system reaches maximum. At equilibrium, sum of all components of entropy change is equal to zero.

$$\sum = 0$$

For the spontaneous reaction which is moving towards equilibrium state, the sum of all components of entropy changes become greater than zero.

$$\sum > 0$$

In steady state condition, macroscopic properties like pressure, composition remain same with time but dissipative process continues to change in a system.

Infinitesimal change in entropy is defined as:-

$$= \quad /$$

For spontaneous process,

$$>$$

Third law of thermodynamics

The third law of thermodynamics states that the entropy of perfect crystal of any pure substance becomes equal to zero when the temperature is absolute zero. At this zero temperature, the system must be in the state possessing minimum thermal energy. This statement is correct only when system has only one state with minimum energy. That is at absolute zero temperature, the state is of perfect order, i.e. zero disorder and hence zero entropy.

$$\lim_{T \rightarrow 0} S = 0$$

The relation between entropy and number of microstates possible for a system is given by:

$$S = k_B \ln \Omega$$

In the above equation  $k_B$  denotes the Boltzmann constant and  $\Omega$  is the thermodynamic probability which is the number of microstates corresponding the given macrostate of the system.

This equation is known as Boltzmann entropy equation. It gives the quantitative definition of entropy as disorder.

1. **Conservation of Mass (Continuity Equation):** The conservation of mass principle states that the total mass of a system remains constant over time, provided there are no mass sources or sinks within the system. In an open system, mass can enter or leave the system through its boundaries. The continuity equation, derived from this principle, expresses the conservation of mass mathematically and is given by:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = S$$

where:

- $\rho$  is the mass density,

- $t$  is time,
- $\mathbf{v}$  is the velocity vector,
- $S$  is the source term (accounts for mass generation or consumption within the system).

This equation states that the rate of change of mass within a control volume is equal to the net rate of mass flow into or out of the volume, plus any mass generation or consumption occurring within the volume.

2. **Conservation of Energy (First Law of Thermodynamics):** The conservation of energy principle, as expressed by the first law of thermodynamics, states that energy cannot be created or destroyed; it can only change forms or be transferred between systems. In an open system, energy can enter or leave the system through various forms such as heat transfer, work done by or on the system, and mass flow carrying energy. The first law of thermodynamics for an open system is expressed as:

$$\frac{dE}{dt} = \dot{Q} - \dot{W} + \sum \dot{m}(h + \frac{1}{2}v^2) + E_{gen}$$

where:

- $E$  is the total energy of the system,
- $\dot{Q}$  is the rate of heat transfer into the system,
- $\dot{W}$  is the rate of work done by the system on its surroundings,
- $\dot{m}$  is the mass flow rate into or out of the system,
- $h$  is the specific enthalpy of the fluid,
- $v$  is the velocity of the fluid,
- $E_{gen}$  is the rate of internal energy generation within the system (due to irreversible processes).

These conservation principles are essential for analyzing and predicting the behavior of open systems undergoing irreversible processes, providing a foundation for understanding fluid dynamics, heat transfer, and chemical reaction engineering.



The expression for entropy production due to heat flow can be derived from the second law of thermodynamics. For a reversible process, the entropy change of a system is given by:

$$\Delta S = Q_{\text{rev}}/T$$

where  $\Delta S$  is the change in entropy,  $Q_{\text{rev}}$  is the heat transfer in a reversible process, and  $T$  is the temperature at which the heat transfer occurs.

For an irreversible process (which is more common in real-world scenarios), the entropy production ( $\Delta S_{\text{irr}}$ ) can be obtained by considering the actual heat transfer  $Q$  and the temperatures  $T_H$  and  $T_C$  of the hot and cold reservoirs respectively:

$$\Delta S_{\text{irr}} = Q/T_C + Q/T_H$$

### Entropy production due to heat flow

The expression shows that entropy production increases with the magnitude of heat transfer and the ratio of heat transfer to temperature. It's important to note that in real processes, entropy production is always positive, reflecting the irreversibility of the process.

Entropy production due to mass transfer can be expressed in terms of the entropy generation rate ( $S_{\text{gen}}$ ) within a control volume. For a steady-state, one-dimensional mass transfer process with no chemical reaction, the entropy generation rate per unit volume ( $s_{\text{gen}}$ ) can be expressed as:

$$s_{\text{gen}} = -\sum_i m_i (s_i + R_i/M_i \ln P_i/P_0)$$

where:

- $\dot{m}_i$  is the mass flow rate of species  $i$ ,
- $s_i$  is the specific entropy of species  $i$ ,
- $R_i$  is the specific gas constant of species  $i$ ,
- $M_i$  is the molar mass of species  $i$ ,
- $P_i$  is the partial pressure of species  $i$ ,
- $P_0$  is the reference pressure.

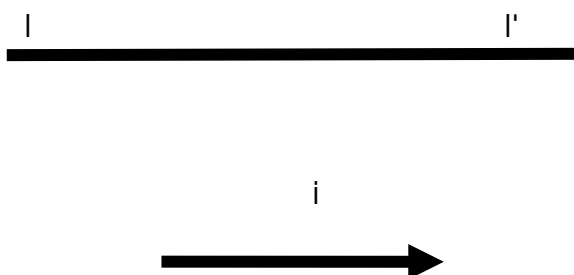
Integrating  $s_{gen}$  over the entire control volume gives the total entropy generation rate ( $\dot{S}_{gen}$ ).

It's important to note that this expression assumes ideal gas behavior and neglects any changes in temperature within the control volume. For more complex situations, additional terms may be necessary to fully account for the entropy generation rate.

### Entropy production due to flow of current in electrical conductor

Let the current of strength  $i$  passes through electric conductor of length  $l$  during a time  $t$ . Then the charge  $i.t$  then flows through a potential difference  $(\phi_{l'} - \phi_l)$  where  $\phi_{l'}$  is potential at  $l'$  and  $\phi_l$  is potential at  $l$ .

Then the electric work done in the process is:  $W_{elec} = i.t(\phi_{l'} - \phi_l)$



**Figure illustrates the direction of flow of current i.e. from I to I'**

According to ohm's law( $\phi' - \phi$ ) can be written as:-

$$\phi' - \phi = -i.R$$

Where R is the resistance of the conductor II'. Since  $\phi' - \phi$  is negative negative sign is represented in above expression.

Substituting eq. we get

$$= - \dots * \dots = -^2$$

Applying first law of thermodynamics;

$$= \Delta + = -^2 \quad (\text{Since there is no change in the system therefore } \Delta U = 0)$$

Similarly, change in entropy  $dS = 0$  for the given system and it is given by

$$dS = dexS + dinS = q / T + dinS$$

Or rearranging the above equation

$$dinS = dS - q / T = -q / T \quad (\text{since } dS = 0)$$

Substituting equation, we get:

$$dinS = -q / T = i^2Rt \quad T > 0$$

Or using equation can be written as:

$$d_i n S = i \cdot t / T (\phi' - \phi) > 0$$

...

(27)

Thus, the electrical force  $1 / T(\phi' - \phi)$  is responsible for the occurrence of flow of charge

i.e. flux i.t.

### **Phenomenological equations and laws**

Phenomenological equations and laws are fundamental principles or relationships that describe the behavior of physical systems based on empirical observations and experimental data. These equations and laws often serve as the foundation for understanding various phenomena in science and engineering. Here are some notable examples across different fields:

The principle of microscopic reversibility states that under equilibrium conditions, any molecular process and its reverse will proceed at the same rate. According to this principle, the rates or velocities of the various types of process (i.e. fluxes) are linearly related to the thermodynamic forces. Thus these forces are responsible for the fluxes that occur. Example,

Force (X) Flux (J)

1. Temperature gradient Heat flow
2. Gradient of chemical potential Diffusion of matter
3. Gradient of electrical potential Flow of charge

In irreversible processes, the transport of heat, mass, momentum and electric charge occurs. In all such cases, a quantity flux is transported as a result of driving force

which is divided from gradient of some physical property of the system. For transport of heat, driving flux is temperature gradient; for transport of mass driving flux is the concentration gradient; for electric current flux is the potential gradient. The transport phenomenon of one dimensional system is:-  $J = LX$  ... (21) Linear law of this kind are referred to as phenomenological law, where J is flux (flow per unit area), X is the driving force (or gradient) which is responsible for the flow and L is proportionality constant called transport coefficient.

**Newton's Law of Universal Gravitation:** Describes the attractive force between two objects with mass. It states that every point mass attracts every other point mass with a force that is directly proportional to the product of their masses and inversely proportional to the square of the distance between their centers.

1. **Newton's Laws of Motion:** These three laws form the basis of classical mechanics. They describe the relationship between the motion of an object and the forces acting on it.

- The first law states that an object will remain at rest or in uniform motion in a straight line unless acted upon by an external force.
- The second law states that the rate of change of momentum of an object is directly proportional to the applied force and takes place in the direction of the force.
- The third law states that for every action, there is an equal and opposite reaction.

Newton's Law: For momentum transfer  $J_M = -\mu du / dx$

2. **Ohm's Law:** Describes the relationship between voltage, current, and resistance in an electrical circuit. It states that the current through a conductor between two points is directly proportional to the voltage across the two points and inversely proportional to the resistance between them.

$$J_e = -\lambda \, dE / dx$$

3. **Fick's Laws of Diffusion:** Describe the process of diffusion, where particles move from areas of high concentration to areas of low concentration. Fick's first law relates the diffusion flux to the concentration gradient, while Fick's second law describes how the concentration of a diffusing substance changes over time.

Fick's Law: For mass transfer

$$J_m = -D \, dc / dx$$

4. **Fourier's Law of Heat Conduction:** Describes the flow of heat through a solid material. It states that the rate of heat transfer through a material is proportional to the negative gradient of the temperature and the area perpendicular to the direction of heat flow.

$$J_Q = -\kappa \, dT / dx$$

5. **Hooke's Law:** Describes the behavior of elastic materials. It states that the force needed to extend or compress a spring by some distance is directly proportional to that distance.

6. **Stefan-Boltzmann Law:** Describes the power radiated from a black body in terms of its temperature. It states that the total energy radiated per unit surface area of a black body is directly proportional to the fourth power of the body's absolute temperature.

In above equations, J is represent corresponding fluxes. i.e.,

$Q_J = \text{heat flux}$

$J_m$  = mass flux

$J_M$  = momentum flux

$J_e$  = electric flux

and  $\kappa$ ,  $D$ ,  $\lambda$ ,  $\mu$  are corresponding transport coefficients which depend upon the material properties of the system. The above laws are called phenomenological laws which are used to define transport processes.

The forces  $X$  drive the flows, a gradient of  $1/T$  causes the flow to heat. But at equilibrium, all the forces and flows vanish. Forces drive the flows, but a flow does not depend entirely on forces; flows can depend on other factors such as presence of catalyst. Catalyst can affect the rate of reaction. When two or more processes occur simultaneously in the same system, it is assumed that each of the flows depend on both the forces which cause the flow.

For small deviation in the forces from their equilibrium value of zero, the flows are expected to be linear function of forces. Lord Rayleigh expressed the linear dependence of all mechanical flows on all mechanical forces in a system.

Deriving phenomenological equations often involves a combination of theoretical considerations, empirical observations, and experimental data analysis. Here's a general outline of the process:

1. **Identify the Phenomenon:** Clearly define the physical phenomenon or behavior you want to describe. This could be anything from heat conduction to fluid flow to chemical reaction rates.
2. **Formulate Hypotheses:** Based on existing knowledge and understanding of the phenomenon, formulate hypotheses or assumptions about the underlying

mechanisms and relationships involved. These hypotheses will guide the derivation process.

3. **Develop a Mathematical Model:** Use mathematical principles, such as conservation laws (mass, energy, momentum), to develop a mathematical model that represents the system under consideration. This model may involve differential equations, integral equations, or other mathematical expressions.
4. **Incorporate Empirical Observations:** Incorporate empirical observations and experimental data into the model. This may involve fitting parameters to experimental data or calibrating the model based on observed behavior.
5. **Validation and Testing:** Validate the derived equations or model by comparing predictions with experimental results. This step may involve further experimentation, sensitivity analysis, or comparison with existing theories.
6. **Refinement and Iteration:** Refine the model based on feedback from validation and testing. This may involve adjusting assumptions, refining parameter values, or incorporating additional factors into the model.
7. **Finalization:** Once the model accurately describes the observed behavior and predictions match experimental results within acceptable tolerances, finalize the phenomenological equations or model.
8. **Application and Extension:** Apply the derived equations or model to new situations or extend it to account for additional factors or complexities. This may involve further research, experimentation, or theoretical development.

It's important to note that the process of deriving phenomenological equations is often iterative and may involve a combination of theoretical reasoning and empirical validation. Additionally, the level of complexity and detail in the model will depend on the specific phenomenon being studied and the desired level of accuracy and predictive capability.



The Onsager reciprocal relations, formulated by Lars Onsager in the early 20th century, are a set of equations that describe the symmetry of transport coefficients in non-equilibrium thermodynamics. These relations establish connections between the coefficients that govern the rates of various transport processes, such as the diffusion of particles, the flow of heat, and the migration of charge.

The central idea behind the Onsager relations is that in a system that is slightly out of equilibrium, the rate of change of one thermodynamic flux (e.g., heat flow) induced by a force (e.g., temperature gradient) is proportional to the difference between that force and the opposing one (e.g., gradient of entropy). Furthermore, these relations dictate that the coefficients relating different pairs of fluxes and forces are symmetric.

The validity of Onsager's theory has been extensively tested and confirmed through both theoretical developments and experimental observations. Here's why the theory is considered valid:

1. **Consistency with Thermodynamics:** The Onsager relations are consistent with the principles of thermodynamics, particularly the second law, which governs the behavior of non-equilibrium systems. They provide a way to extend thermodynamic principles to systems far from equilibrium.
2. **Experimental Confirmation:** Numerous experimental studies have verified the predictions of Onsager's theory in various physical systems, including electrical conductivity in electrolytes, thermal conductivity in fluids, and diffusion processes in solutions.
3. **Mathematical Rigor:** The mathematical framework of Onsager's theory is solid and has been rigorously developed within the context of statistical mechanics and linear response theory. The theory provides a systematic approach to deriving the relationships between transport coefficients.
4. **Predictive Power:** Onsager's reciprocal relations have proven to be powerful tools for predicting and understanding the behavior of complex systems under non-

equilibrium conditions. They provide quantitative relationships between different transport phenomena, allowing for the calculation of transport coefficients from measurable quantities.

While Onsager's theory has been remarkably successful in explaining and predicting the behavior of many physical systems, it does have limitations. For instance, it is based on linear response theory, which is valid only for small deviations from equilibrium. Additionally, it may not apply in systems that exhibit strong nonlinearities or when there are spatial inhomogeneities. Nonetheless, within its domain of applicability, the Onsager reciprocal relations remain a cornerstone of non-equilibrium thermodynamics and continue to be widely used in theoretical and experimental studies.

Electrokinetic and thermomechanical effects are phenomena that involve the coupling between electrical, mechanical, and thermal processes in various materials and systems. Here's an overview of each:

### 1. **Electrokinetic Effects:**

Electrokinetic effects refer to the interaction between electrical fields and fluid flow in porous media or electrically charged surfaces. These effects are particularly relevant in fields such as electrochemistry, colloid science, and microfluidics. Some key electrokinetic phenomena include:

- **Electrophoresis:** The movement of charged particles suspended in a fluid under the influence of an electric field. The particles migrate towards the electrode of opposite charge.
- **Electroosmosis:** The motion of a fluid (typically water) through a porous medium or microchannel under the influence of an applied electric field. This effect is often utilized in microfluidic devices for pumping fluids without mechanical parts.

- **Electrothermal Effects:** The generation of heat due to the interaction between electrical currents and the resistance of a conducting medium. This can lead to temperature gradients and associated fluid flow, known as thermoelectric convection.

## 2. Thermomechanical Effects:

Thermomechanical effects involve the coupling between temperature and mechanical properties in materials. These effects are significant in various engineering applications, including materials science, solid mechanics, and thermal management. Some notable thermomechanical phenomena include:

- **Thermal Expansion:** Changes in dimensions (length, volume) of a material in response to temperature changes. Different materials exhibit different coefficients of thermal expansion, which can lead to stress and strain within a structure.
- **Thermoelasticity:** The coupling between temperature and elastic deformation in materials. Heating or cooling a material can induce stresses and strains, affecting its mechanical behavior.
- **Thermal Stress:** The stresses induced in a material due to temperature gradients. Differential expansion or contraction across different parts of a structure can lead to thermal stresses, which can potentially cause deformation or failure.

Electrokinetic and thermomechanical effects are often interconnected in practical systems. For example, in electrokinetic flows through microchannels, the Joule heating due to electrical currents can lead to temperature gradients, which in turn affect fluid flow patterns. Understanding and controlling these coupled phenomena are crucial in various technological applications, including microfluidics, electrochemical devices, and thermal management systems

## **Application of irreversible thermodynamics to biological systems**

Irreversible thermodynamics, a branch of thermodynamics that deals with systems far from equilibrium, has found numerous applications in biological systems. Here are some key areas where irreversible thermodynamics is applied in biology:

1. **Bioenergetics:** Irreversible thermodynamics provides a framework for understanding the flow of energy in biological systems, particularly in processes such as cellular respiration and photosynthesis. By considering energy dissipation and entropy production, irreversible thermodynamics can explain the efficiency and limitations of biological energy conversion processes.
2. **Membrane Transport:** Biological membranes play crucial roles in controlling the transport of ions, molecules, and other substances across cellular boundaries. Irreversible thermodynamics helps describe the mechanisms of transport phenomena such as diffusion, osmosis, and active transport, providing insights into the energetics and kinetics of these processes.
3. **Metabolic Networks:** Metabolic pathways in living organisms involve complex networks of biochemical reactions. Irreversible thermodynamics can be used to analyze metabolic fluxes and optimize metabolic pathways for energy production, growth, and other cellular functions. This approach, known as metabolic flux analysis, has applications in metabolic engineering and biotechnology.
4. **Heat Dissipation:** Living organisms generate heat as a byproduct of metabolic processes. Irreversible thermodynamics helps explain how organisms dissipate heat to maintain thermal equilibrium with their surroundings. This is particularly relevant in the context of thermoregulation and the adaptation of organisms to different environmental conditions.
5. **Molecular Motors:** Biological molecular motors, such as ATP synthase and kinesin, convert chemical energy into mechanical work. Irreversible thermodynamics provides insights into the thermodynamic efficiency and kinetics of these molecular machines, helping elucidate their mechanisms of action and physiological roles.

6. **Biological Growth and Development:** The growth and development of biological organisms involve a series of irreversible processes, including cell proliferation, differentiation, and morphogenesis. Irreversible thermodynamics can be used to model and analyze these processes, shedding light on the underlying principles governing biological growth and development.
7. **Biological Information Processing:** Biological systems exhibit remarkable information processing capabilities, such as signal transduction, gene regulation, and neural processing. Irreversible thermodynamics provides a theoretical framework for understanding the thermodynamic constraints and optimization principles underlying these complex processes.

Overall, the application of irreversible thermodynamics to biological systems has led to significant advancements in our understanding of the fundamental principles governing living organisms and has practical implications in fields such as biophysics, biochemistry, and systems biology.

## UNIT-IV

### Kinetics of Reactions

Theories of reactions provide frameworks for understanding and predicting chemical reactions at the molecular level. Here are some notable theories:

1. **Collision Theory:** Collision theory provides a qualitative explanation of reaction rates based on the collision of reactant molecules. According to this theory, for a reaction to occur, reactant molecules must collide with sufficient energy and proper orientation. The rate of a reaction is proportional to the frequency of collisions and the fraction of collisions with sufficient energy and correct orientation. While collision theory is useful for understanding reaction kinetics, it does not account for factors such as molecular structure and energy distribution.

Collision theory provides a qualitative explanation of reaction rates by considering the collisions between reactant molecules. The theory suggests that for a chemical reaction to occur, reactant molecules must collide with sufficient energy and proper orientation. Here's a basic derivation of the collision theory:

### Assumptions:

1. **Reactant particles are in constant motion:** Reactant particles are assumed to be in constant motion due to thermal energy.
2. **Collisions lead to reaction:** Only a fraction of collisions between reactant molecules result in a chemical reaction. This fraction is determined by the energy and orientation of the collision.

### Derivation:

#### 1. Number of Collisions:

Consider  $N_A$  and  $N_B$  as the number of molecules of reactants A and B respectively, per unit volume.

The number of collisions per unit time between A and B molecules is given by:

$$Z = N_A \times N_B \times \text{collision frequency}$$

The collision frequency is determined by the speed of the molecules and the cross-sectional area for collision.

#### 2. Effective Collisions:

Not all collisions lead to a reaction. Only those collisions where the molecules have sufficient energy and proper orientation will result in a reaction. Let's define an effective collision frequency  $Z_{\text{eff}}$  to account for this:

$$Z_{\text{eff}} = Z \times P_{\text{collision}} \times P_{\text{orientation}}$$

- $P_{\text{collision}}$  is the probability factor related to the energy of the collision.

- *P*orientation is the probability factor related to the proper orientation of the colliding molecules.

### 3. Reaction Rate:

The rate of the reaction is proportional to the number of effective collisions per unit time. Let  $k$  be the rate constant for the reaction, then the rate of the reaction ( $R$ ) is given by:

$$R = k \times Z_{\text{eff}}$$

Substituting  $Z_{\text{eff}}$  from above:

$$R = k \times Z \times P_{\text{collision}} \times P_{\text{orientation}}$$

### 4. Arrhenius Formulation:

Considering the energy dependence of the collision probability, we can express  $P_{\text{collision}}$  in terms of the Arrhenius equation:

$$P_{\text{collision}} = e^{-E_a/RT}$$

Where:

- $E_a$  is the activation energy,
- $R$  is the gas constant,
- $T$  is the temperature in Kelvin.

### 5. Overall Rate Expression:

Substituting  $P_{\text{collision}}$  into the rate expression, we get:

$$R = k \times Z \times e^{-E_a/RT} \times P_{\text{orientation}}$$

The term  $P_{\text{orientation}}$  accounts for the fraction of collisions with the proper orientation for reaction. This term is determined empirically or by quantum mechanical calculations for specific reactions.

This is a simplified derivation of the collision theory, which provides a basic understanding of how reaction rates are related to collision frequencies and probabilities. More complex versions of collision theory may include considerations such as molecular size, shape, and intermolecular forces.



**Transition State Theory (TST):** Transition state theory builds upon collision theory by considering the formation of an activated complex, or transition state, during a reaction. This theory provides a more detailed description of reaction rates by incorporating the concept of a potential energy surface, which represents the energy changes as reactants progress to products. Transition state theory allows for the calculation of rate constants and provides insights into the factors that influence reaction rates, such as temperature and activation energy.

Transition State Theory (TST) provides a more detailed understanding of reaction rates by considering the formation of an activated complex, or transition state, during a chemical reaction. It builds upon the concept of a potential energy surface, which represents the energy changes as reactants progress to products. Here's a detailed explanation of Transition State Theory:

#### **Assumptions:**

1. **Assuming Equilibrium:** TST assumes that at the transition state, the system is in equilibrium with the reactants and products.
2. **Steady-State Approximation:** TST assumes that the rate of formation of the activated complex is equal to its rate of decomposition, maintaining a steady-state concentration.

#### **Derivation:**

##### 1. **Reaction Coordinate:**

Let's consider a chemical reaction where reactants  $A$  and  $B$  combine to form products  $C$  and  $D$ . The progress of the reaction can be represented by a reaction coordinate,  $s$ , which describes the progress from reactants to products.

##### 2. **Potential Energy Surface (PES):**

The potential energy surface  $V(s)$  represents the energy changes as the reaction progresses along the reaction coordinate. At the transition state, the potential energy reaches a maximum, representing the activation energy barrier.

### 3. Rate Constant Expression:

According to transition state theory, the rate constant  $k$  for the reaction can be expressed as:

$$k = h k_B / T \times e^{-\Delta G^\ddagger / RT} \quad \text{Where:}$$

- $k_B$  is the Boltzmann constant,
- $T$  is the temperature in Kelvin,
- $h$  is Planck's constant,
- $\Delta G^\ddagger$  is the Gibbs free energy of activation,
- $R$  is the gas constant.

### 4. Gibbs Free Energy of Activation:

The Gibbs free energy of activation ( $\Delta G^\ddagger$ ) can be related to the enthalpy of activation ( $\Delta H^\ddagger$ ) and the entropy of activation ( $\Delta S^\ddagger$ ):  $\Delta G^\ddagger = \Delta H^\ddagger - T\Delta S^\ddagger$

### 5. Frequency Factor:

The frequency factor ( $A$ ) is related to the pre-exponential factor in the Arrhenius equation and accounts for the frequency of collisions and the probability of the correct orientation of reactant molecules at the transition state.

### 6. Arrhenius Equation:

Combining the rate constant expression and the frequency factor, we get the Arrhenius equation:

$$k = A \times e^{-RT/\Delta G^\ddagger}$$

Transition State Theory provides a theoretical framework for understanding reaction rates by considering the formation of an activated complex and the energy barrier associated with the transition state. It allows for the calculation of rate constants based on the thermodynamic properties of the transition state and provides insights

into the factors that influence reaction rates, such as temperature and activation energy.

### **Effect of temperature on reaction rates**

The effect of temperature on reaction rates is described by the Arrhenius equation, which is derived from transition state theory and collision theory. The Arrhenius equation relates the rate constant ( $k$ ) of a chemical reaction to temperature ( $T$ ) and the activation energy ( $E_a$ ). Here's how temperature affects reaction rates:

#### **Arrhenius Equation:**

The Arrhenius equation is given by:  $k = A \times e^{-E_a/RT}$

Where:

- $k$  is the rate constant,
- $A$  is the pre-exponential factor or frequency factor,
- $E_a$  is the activation energy,
- $R$  is the gas constant,
- $T$  is the temperature in Kelvin.

#### **Effect of Temperature:**

##### **1. Increase in Temperature:**

- As temperature increases, the exponential term in the Arrhenius equation ( $e^{-E_a/RT}$ ) becomes smaller, leading to an increase in the rate constant ( $k$ ).
- Higher temperatures provide reactant molecules with more kinetic energy, increasing the likelihood of successful collisions and overcoming the activation energy barrier.

##### **2. Activation Energy:**

- The activation energy ( $E_a$ ) represents the energy barrier that reactant molecules must overcome to form the transition state and proceed to product formation.
- Increasing temperature effectively provides more thermal energy to the reactant molecules, making it easier to overcome the activation energy barrier and increasing the reaction rate.

### 3. Temperature Dependence:

- The dependence of reaction rate on temperature is exponential, as shown in the Arrhenius equation.
- A small change in temperature can have a significant effect on the reaction rate, especially at higher temperatures where the exponential term becomes more pronounced.

### 4. Reaction Kinetics:

- The effect of temperature on reaction rates is fundamental to understanding reaction kinetics and is essential for designing and optimizing chemical processes.
- Reaction rates typically double or triple for every 10°C increase in temperature, known as the "temperature coefficient" or "Q10" value.
- 

Temperature plays a critical role in determining reaction rates by influencing the kinetic energy of reactant molecules and their ability to overcome the activation energy barrier. Understanding the temperature dependence of reaction rates is essential for controlling reaction kinetics and optimizing chemical processes in various fields, including chemistry, biochemistry, and engineering.

### **Lindemann theory of unimolecular reactions**

The Lindemann theory of unimolecular reactions, proposed by Peter Lindemann in 1920, provides an explanation for the rate of reaction for processes involving the dissociation of a single molecule into two or more products. This theory is particularly relevant for gas-phase reactions and is based on the concept of collision theory. Here's an overview of the Lindemann theory:

### Assumptions:

1. **Molecular Collisions:** Lindemann's theory assumes that the rate of a unimolecular reaction is determined by collisions between molecules in the gas phase.
2. **Energy Transfer:** The theory considers that energy is transferred between colliding molecules during these collisions.
3. **Activated Complex Formation:** It assumes that a reactive intermediate, known as the activated complex or transition state, forms during collisions between reactant molecules.

### Derivation:

#### 1. Reaction Mechanism:

Consider a unimolecular reaction  $A \rightarrow B + C$ , where  $A$  is the reactant molecule and  $B$  and  $C$  are the products. The overall reaction rate can be expressed as:

$$R = k_{uni}[A]$$

Where  $k_{uni}$  is the rate constant for the unimolecular reaction and  $[A]$  is the concentration of the reactant molecule  $A$ .

#### 2. Collision Frequency:

According to collision theory, the collision frequency ( $Z$ ) between molecules can be expressed as:

$$Z = \pi \mu \sqrt{8kT}$$

Where:

- $k$  is Boltzmann's constant,
- $T$  is the temperature in Kelvin,
- $\mu$  is the reduced mass of the colliding molecules.

### 3. Probability of Reaction:

The probability of reaction ( $P$ ) during a collision is assumed to be proportional to the fraction of collisions with sufficient energy to form the activated complex. This can be expressed as:

$$P = e^{-E_a/RT}$$

Where:

- $E_a$  is the activation energy,
- $R$  is the gas constant.

### 4. Rate Constant:

The rate constant for the unimolecular reaction can be expressed as the product of the collision frequency ( $Z$ ) and the probability of reaction ( $P$ ):

$$k_{uni} = Z \times P$$

Substituting the expressions for  $Z$  and  $P$ , we get:

$$k_{uni} = \pi \mu \sqrt{8kT} \times e^{-RTE_a}$$

The Lindemann theory of unimolecular reactions provides a theoretical framework for understanding the rate of dissociation reactions in the gas phase. It demonstrates how the rate constant for a unimolecular reaction depends on factors such as temperature, collision frequency, and activation energy. While the Lindemann theory has been successful in explaining the behavior of certain gas-phase reactions, it has limitations and does not account for factors such as molecular orientation and steric effects. More sophisticated theories, such as transition state theory, provide a more accurate description of reaction rates in complex systems.

:

### **Lindeman and Christiansen Hypothesis:**

The Lindeman and Christiansen hypothesis, also known as the Lindeman mechanism or the Lindeman cycle, is a theory proposed to explain the mechanism of combustion reactions, particularly in the context of hydrocarbon fuels. This hypothesis was developed by H. A. Lindeman and J. A. Christiansen in the 1920s. Here's an overview

1. **Overview:** The Lindeman and Christiansen hypothesis proposes a chain reaction mechanism for the combustion of hydrocarbon fuels, such as methane, propane, or gasoline.

2. **Chain Reaction:**

- The combustion process is initiated by the decomposition of the fuel molecule into radicals (highly reactive species with unpaired electrons) through the input of energy, typically in the form of heat or light.
- These radicals then react with oxygen molecules ( $O_2$ ) in the air to form stable combustion products (water, carbon dioxide) and more radicals.
- The newly formed radicals continue to propagate the chain reaction by reacting with additional fuel molecules, leading to a self-sustaining combustion process.

3. **Termination:**

- The combustion chain reaction is terminated through various mechanisms, such as radical-radical recombination or the depletion of fuel and oxygen.

#### 4. Reaction Steps:

- The Lindeman and Christiansen hypothesis describes several key steps in the combustion chain reaction, including initiation, propagation, branching, and termination.
- Initiation involves the initial decomposition of fuel molecules into radicals.
- Propagation involves the sequential reaction of radicals with oxygen molecules to form stable products and additional radicals.
- Branching refers to the branching reactions where radicals react with other radicals to form new species.
- Termination involves the processes that bring the chain reaction to an end, such as radical recombination or fuel depletion.

#### Significance:

- The Lindeman and Christiansen hypothesis provides a conceptual framework for understanding the mechanism of combustion reactions and the role of radical species in the combustion process.
- It helps explain the observed behavior of combustion reactions, including the self-sustaining nature of flames and the formation of combustion products.
- The hypothesis has practical applications in combustion engineering, where it is used to design and optimize combustion systems for various applications, including engines, furnaces, and power plants.

Overall, the Lindeman and Christiansen hypothesis is an important concept in the study of combustion science, providing insights into the complex chemistry and kinetics of combustion reactions in hydrocarbon fuels.



Molecular beams, collision cross sections, and the effectiveness of collisions are fundamental concepts in the study of gas-phase reactions and collision dynamics. Here's an overview of each:

### **Molecular Beams:**

1. **Definition:** Molecular beams are directed, collimated streams of gas-phase molecules traveling at controlled velocities and angles. They are typically produced using specialized apparatus such as supersonic expansion nozzles or effusive sources.

2. **Applications:**

- Molecular beams are used in various experimental techniques, including:
  - Scattering experiments to study collision dynamics and surface interactions.
  - Laser spectroscopy to probe molecular energy levels and structure.
  - Gas-phase reaction kinetics to investigate reaction mechanisms and rates.
- They are also used in surface science to study adsorption, desorption, and surface reactions.

### **Collision Cross Sections:**

1. **Definition:** Collision cross section ( $\sigma$ ) is a measure of the effective area that a molecule presents to another molecule during a collision. It represents the probability of a collision occurring when two molecules come into contact.

2. **Calculation:**

- Collision cross sections can be calculated theoretically using quantum mechanical methods or estimated experimentally using techniques such as crossed molecular beam experiments or gas-phase scattering experiments.

- The collision cross section depends on factors such as the size, shape, and internal energy of the colliding molecules, as well as their relative velocities and orientations.

### 3. **Significance:**

- Collision cross sections are essential for understanding gas-phase reactions and collision dynamics, as they determine the likelihood of collisions leading to chemical reactions or scattering events.
- They play a crucial role in modeling and simulating gas-phase processes, such as molecular diffusion, reaction rates, and transport phenomena.

### **Effectiveness of Collisions:**

1. **Definition:** The effectiveness of collisions refers to the ability of collisions between molecules to result in a desired outcome, such as chemical reaction, energy transfer, or scattering.

#### 2. **Factors Affecting Effectiveness:**

- **Energy:** Collisions must possess sufficient energy to overcome activation barriers for chemical reactions or to induce energy transfer processes.
- **Orientation:** Collisions must occur with the proper orientation to promote specific interactions or reactions.
- **Collision Cross Section:** The larger the collision cross section, the higher the probability of an effective collision occurring.
- **Collision Frequency:** The frequency of collisions between molecules influences the overall effectiveness of collisions.

#### 3. **Control and Optimization:**

- Understanding and controlling the factors that affect the effectiveness of collisions are essential for optimizing reaction conditions and enhancing reaction rates in various applications, such as chemical synthesis, catalysis, and plasma processing.

- Experimental techniques, theoretical models, and computational simulations are used to study and manipulate collision dynamics to achieve desired outcomes.

Molecular beams, collision cross sections, and the effectiveness of collisions are key concepts in the study of gas-phase reactions and collision dynamics, with important implications for various fields of science and technology.

The Analysis of Relaxation and Reaction Times (ARRT) is a valuable experimental technique used to study the kinetics of chemical reactions, particularly those involving short-lived intermediates and fast reaction rates. ARRT provides insights into the reaction mechanism, reaction kinetics, and the identification of reactive intermediates. Here are some applications of ARRT to reactions between atoms and molecules, along with the evaluation of time and true order-kinetic parameters:

### **1. Studying Fast Reactions:**

- ARRT is particularly useful for studying fast reactions where conventional methods may not provide sufficient temporal resolution.
- By monitoring the relaxation and reaction times, ARRT can elucidate the kinetics of rapid chemical processes, including reactions involving atoms and molecules with short lifetimes.

### **2. Mechanistic Studies:**

- ARRT can provide information about reaction mechanisms by observing the transient behavior of intermediates.
- By analyzing the relaxation and reaction times, researchers can infer the sequence of elementary steps involved in the reaction mechanism.

### **3. Transient Species Identification:**

- ARRT enables the detection and characterization of transient species, such as radicals, ions, and excited states, which play crucial roles in chemical reactions.
- By correlating relaxation times with the lifetimes of transient species, ARRT can aid in the identification and quantification of reactive intermediates.

#### **4. Temperature Dependence Studies:**

- ARRT experiments conducted at different temperatures can provide insights into the temperature dependence of reaction rates.
- By varying the temperature and analyzing the relaxation and reaction times, researchers can determine the activation energy and pre-exponential factor of the reaction.

#### **5. True Order-Kinetic Parameter Evaluation:**

- ARRT allows for the determination of true order kinetics, especially for complex reactions where the order of the reaction may vary with time or reactant concentration.
- By analyzing the time dependence of relaxation and reaction processes, researchers can evaluate the true order of the reaction and identify any deviations from simple kinetics.

#### **6. Reaction Rate Constants Determination:**

- ARRT facilitates the determination of reaction rate constants for fast reactions by providing accurate measurements of relaxation and reaction times.
- By fitting experimental data to kinetic models, researchers can extract rate constants and rate laws that describe the kinetics of the reaction.

#### **7. Kinetic Modeling Validation:**

- ARRT data can be used to validate kinetic models and theoretical predictions of reaction kinetics.
- By comparing experimental results with model predictions, researchers can refine kinetic models and improve their accuracy in describing complex reaction mechanisms.

ARRT is a versatile experimental technique with various applications in the study of reactions between atoms and molecules. By providing insights into reaction kinetics, mechanisms, and transient species identification, ARRT contributes to our understanding of chemical processes occurring on short timescales.

Time and true order-kinetic parameter evaluation refers to the determination of reaction kinetics parameters, such as reaction order and rate constants, accurately over time and under conditions where the reaction may not follow simple first-order or second-order kinetics. Here's a deeper look at how this evaluation is conducted:

#### **Time-Dependent Kinetic Parameter Evaluation:**

1. **Dynamic Behavior Observation:** Initially, the reaction progress is monitored over time to observe how the concentrations of reactants and products change. This can be done using various analytical techniques such as spectroscopy, chromatography, or electrochemistry.
2. **Data Analysis:** The time-dependent concentration data obtained from the experiment is then analyzed using mathematical models to extract kinetic parameters. This analysis may involve fitting the data to various kinetic models, such as first-order, second-order, or complex reaction models.
3. **Kinetic Model Selection:** The appropriate kinetic model is selected based on the experimental data and the mechanistic understanding of the reaction. This involves

considering factors such as the nature of reactants, reaction mechanism, and experimental conditions.

4. **Parameter Estimation:** Using the selected kinetic model, the rate constants and reaction orders are estimated by fitting the experimental data to the model equations. This estimation can be done using regression analysis or numerical methods.

5. **Model Validation:** The validity of the selected kinetic model and the estimated parameters is assessed by comparing the model predictions with experimental observations. Good agreement between the model and experimental data indicates the reliability of the parameters.

#### **True Order-Kinetic Parameter Evaluation:**

1. **Time-Dependent Reaction Order Determination:** In cases where the reaction order changes over time or with changing reactant concentrations, the true order of the reaction is evaluated experimentally. This involves monitoring the reaction rate at different reactant concentrations and over different time intervals.

2. **Initial Rate Method:** The initial rates of the reaction are measured at various initial reactant concentrations. The observed initial rates are then used to determine the reaction order with respect to each reactant.

3. **Integral Method:** Alternatively, the integral method can be used to determine the reaction order. This involves integrating the rate equations for different reaction orders and fitting the resulting integrated rate expressions to experimental data to determine the best-fit reaction order.

4. **Time-Dependent Rate Constant Determination:** The rate constants for the reaction are determined experimentally at different reaction times and under various conditions. This allows for the evaluation of how the rate constant changes over time and with changing reaction conditions.

5. **Model Refinement:** Based on the determined reaction order and rate constants, the kinetic model is refined to accurately describe the time-dependent behavior of the reaction. This may involve modifying the kinetic mechanism or considering additional reaction pathways.

By performing time and true order-kinetic parameter evaluation, researchers can gain a comprehensive understanding of the kinetics of complex reactions and accurately describe their behavior over time and under various conditions. This information is crucial for optimizing reaction conditions, predicting reaction behavior, and designing efficient chemical processes.

### **Factors determine the rate of reaction**

The rate of a chemical reaction in solution depends on various factors that influence the frequency and effectiveness of molecular collisions between reactant molecules.

These factors can be broadly categorized into:

#### **1. Nature of Reactants:**

1. **Chemical Nature:** The chemical structure and properties of the reactants determine their reactivity. For example, reactions involving highly reactive species or species with labile bonds tend to proceed faster.

2. **Concentration:** The concentration of reactants in solution directly affects the rate of reaction. Higher concentrations lead to more frequent collisions between reactant molecules, increasing the reaction rate according to the rate law.

## 2. Reaction Conditions:

1. **Temperature:** Temperature significantly influences reaction rates. Higher temperatures increase the kinetic energy of molecules, leading to more frequent and energetic collisions. The reaction rate typically doubles for every 10°C rise in temperature due to the Arrhenius equation.

2. **Pressure (for gas-phase reactions):** In gas-phase reactions, pressure affects the concentration of reactant molecules. Increased pressure leads to higher concentrations of gas molecules, resulting in more frequent collisions and faster reaction rates.

3. **Solvent:** The nature and properties of the solvent can affect the reaction rate. For example, polar solvents may stabilize ionic species and enhance their reactivity, while non-polar solvents may hinder reaction rates for polar reactants.

4. **Catalysts:** Catalysts increase the rate of reaction by providing an alternative reaction pathway with lower activation energy. They do not alter the equilibrium position but can significantly increase the rate of the forward and reverse reactions.

## 3. Reaction Mechanism:

1. **Activation Energy:** The energy barrier that reactant molecules must overcome to form products influences the reaction rate. Reactions with lower activation energies proceed faster.



2. **Reaction Order:** The order of the reaction with respect to each reactant affects the overall rate law. The rate expression provides information on how changes in reactant concentrations impact the reaction rate.

3. **Complexity of the Reaction:** Complex reactions involving multiple steps, intermediates, and transition states may proceed at different rates depending on the rate-determining step.

#### 4. Physical Factors:

1. **Surface Area:** For reactions involving solids, increasing the surface area of the reactants can enhance the rate of reaction by exposing more reactant molecules to the reaction sites.

2. **Stirring or Agitation:** Stirring or agitation of the reaction mixture increases the mixing of reactants, leading to more collisions and faster reaction rates.

3. **Presence of Light:** Photochemical reactions are influenced by the intensity and wavelength of light. Light can provide the energy needed to overcome activation barriers, leading to increased reaction rates.

By considering these factors, researchers can predict and manipulate the rates of chemical reactions in solution, allowing for the optimization of reaction conditions and the development of efficient chemical processes.

#### Primary and secondary salt effects

Primary and secondary salt effects are phenomena observed in the kinetics of reactions in solution, particularly those involving ionic species. These effects arise due to the presence of additional ions (salts) in the reaction mixture, which can influence the reaction rate through various mechanisms. Here's an overview of primary and secondary salt effects along with their expressions:

### 1. Primary Salt Effect:

The primary salt effect refers to the influence of the concentration of a primary salt (an electrolyte) on the rate of a reaction. It occurs when the primary salt directly interacts with the reactants or affects the reaction mechanism.

**Expression:** The primary salt effect is often expressed using the empirical equation known as the Bürgi-Dunitz equation:

$$\log(k/k_0) = \alpha \cdot m + \beta \cdot m^{1/2}$$

Where:

- $k$  is the rate constant in the presence of the salt,
- $k_0$  is the rate constant in the absence of the salt,
- $m$  is the molality (moles of salt per kilogram of solvent),
- $\alpha$  and  $\beta$  are coefficients representing the primary and secondary salt effects, respectively.

### 2. Secondary Salt Effect:

The secondary salt effect refers to the influence of the concentration of a secondary salt (an additional electrolyte) on the rate of a reaction. It occurs when the secondary salt affects the ionic strength or ionic environment of the solution, indirectly influencing the reaction rate.

**Expression:** The secondary salt effect is often incorporated into the rate equation through the Debye-Hückel equation or other ionic strength correction terms. The rate equation can be modified to include the effect of the secondary salt as follows:

$$k = k_0 \times f(I)$$

Where:

- $k$  is the rate constant in the presence of the secondary salt,
- $k_0$  is the rate constant in the absence of the secondary salt,
- $f(I)$  is the ionic strength correction factor, which depends on the total ionic strength of the solution.

### Interpretation:

#### 1. Primary Salt Effect:

- The primary salt effect arises due to specific interactions between the electrolyte ions and the reactants or transition states of the reaction.
- The coefficients  $\alpha$  and  $\beta$  provide information about the nature and strength of these interactions.

#### 2. Secondary Salt Effect:

- The secondary salt effect arises due to changes in the ionic strength or electrostatic environment of the solution caused by the additional electrolyte.
- The effect of the secondary salt can be quantified using the Debye-Hückel equation or other ionic strength correction terms.

### Applications:

#### 1. Primary Salt Effect:

- Used to investigate the mechanism of reactions involving ionic species and to understand ion-reactant interactions.

- 

## 2. Secondary Salt Effect:

- Important in the study of reaction kinetics in complex solutions containing multiple electrolytes, such as biological or environmental systems.

Understanding the primary and secondary salt effects is crucial for accurately predicting and controlling reaction rates in solution, especially in systems where electrolyte concentrations vary or where reactions occur in the presence of multiple ionic species

## Potential energy surface

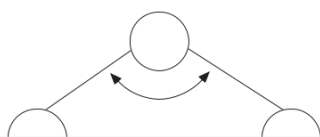
A dynamical study of molecular collisions requires construction of the Hamiltonian  $H = T + V$ , where  $T$  and  $V$  are kinetic energy (KE) and potential energy (PE), respectively. A knowledge of the interaction potential, therefore, is essential for the study of molecular dynamics.

The potential energy of a diatomic molecule depends on only the distance between two bonded atoms. The potential energy of a diatomic molecule can be plotted in two dimensions by plotting PE as a function of the bond length. The curve is known as *potential energy curve*.

When potential energy depends on more than one geometric parameter, i.e. internuclear distances, the word surface is used in place of curve, and the plot is known as *potential energy surface* (PES).

For a nonlinear molecule consisting of  $N$  atoms, the potential energy surface depends on  $3N - 6$  independent coordinates and depicts how the PE changes as relative coordinates of the atomic nuclei involved in the chemical reaction are varied. For example, consider the water molecule. The potential energy of water molecule is a function of three parameters, i.e.  $r_1$ ,  $r_2$  and angle  $\theta$ . A plot of the complete potential energy surface of a water molecule, therefore, will be four dimensional. Since we are limited to three dimensions for plotting functions, we cannot draw the entire potential energy surface of a water molecule in a single plot. However, we can draw parts of PES. Let if one geometric parameter, say  $\theta$ , has been fixed, then potential energy will be a function of  $r_1$  and  $r_2$  at constant  $\theta$ , and the plot will be a three dimensional. Such a plot is a cross sectional cut of the full potential surface. A cross sectional plot shows how the PE of molecule changes on variation of the some geometric variables while holding the other constant.

Potential energy surface for a chemical reaction can be obtained using electronic structure techniques or by solving Schrödinger equation within Born-Oppenheimer approximation. For each geometry, there is a PE value of the system.



## 1. Potential Energy:

- The vertical axis represents potential energy ( $E$ ), which is the energy of the system at each point along the reaction coordinate.
- The potential energy surface describes how the potential energy of the system changes as the reaction progresses.

## 2. Reaction Coordinate:

- The horizontal axis represents the reaction coordinate ( $s$ ), which describes the progress of the reaction from reactants to products.
- The reaction coordinate can represent various aspects of the reaction, such as bond breaking, bond forming, or molecular rearrangement.

## 3. Energy Barrier:

- The highest point on the potential energy surface corresponds to the activation energy barrier ( $E_a$ ), which reactant molecules must overcome to proceed to product formation.
- The energy barrier separates the reactants from the transition state, where the bonds are in the process of breaking and forming.

## 4. Reactants and Products:

- The left side of the diagram represents the reactants, which are the initial molecular configurations before the reaction occurs.
- The right side of the diagram represents the products, which are the final molecular configurations after the reaction has occurred.

## 5. Transition State:

- The transition state is the point along the reaction coordinate corresponding to the highest potential energy.
- It represents the configuration of the reacting molecules at the peak of the energy barrier.
- At the transition state, bonds are in the process of breaking and forming, and reactant molecules are undergoing chemical transformation.

The potential energy surface provides insights into the energetics and kinetics of chemical reactions, including the activation energy barrier, reaction mechanism, and stability of reactants and products. It is a fundamental concept in the study of reaction dynamics and plays a crucial role in understanding and predicting chemical reactions.

## Homogeneous catalysis

Homogeneous catalysis is a process in which the catalyst and the reactants are present in the same phase, typically in the same solution. In homogeneous catalysis, the catalyst undergoes the same physical state as the reactants and products throughout the reaction. This allows for close interaction between the catalyst and the reactants, facilitating the catalytic process. Here's an overview of homogeneous catalysis:

### Mechanism of Homogeneous Catalysis:

1. **Formation of Catalytic Complex:** The catalyst reacts with the reactants to form a catalytic complex. This complex lowers the activation energy required for the reaction to proceed.
2. **Reaction Facilitation:** The catalytic complex stabilizes transition states or intermediates, enabling faster reaction rates or alternative reaction pathways.
3. **Regeneration of Catalyst:** At the end of the reaction, the catalyst is regenerated and can participate in subsequent reaction cycles without being consumed.

### Examples of Homogeneous Catalysts:

1. **Transition Metal Complexes:** Transition metal complexes, such as those of platinum, palladium, ruthenium, and rhodium, are widely used as homogeneous catalysts in various organic transformations. For example, Wilkinson's catalyst ( $\text{RhCl}(\text{PPh}_3)_3$ ) is used in hydrogenation reactions.
2. **Organometallic Compounds:** Organometallic compounds, such as Grubbs' catalyst ( $\text{RuCl}_2(\text{PPh}_3)_3$ ), are used in olefin metathesis reactions.
3. **Enzymes:** Enzymes are biological catalysts that often operate homogeneously in solution. They catalyze a wide range of biochemical reactions in living organisms.

### Advantages of Homogeneous Catalysis:

1. **High Activity:** Homogeneous catalysts can exhibit high catalytic activity due to their close interaction with reactant molecules.
2. **Selectivity:** Homogeneous catalysts can often be tailored to provide high selectivity for specific reaction pathways, leading to fewer side reactions and higher product yields.
3. **Mild Reaction Conditions:** Many homogeneous catalytic reactions can be performed under mild conditions of temperature and pressure, reducing energy consumption and environmental impact.

### Challenges of Homogeneous Catalysis:

1. **Product Separation:** Separation of the catalyst from the reaction mixture can be challenging, especially for highly soluble catalysts. This can affect product purity and increase processing costs.



2. **Catalyst Stability:** Some homogeneous catalysts may be sensitive to reaction conditions or susceptible to deactivation, requiring careful optimization of reaction parameters.

3. **Catalyst Recovery and Recycling:** The recovery and recycling of homogeneous catalysts can be difficult and costly, particularly for catalysts that are prone to degradation or contamination.

### **Applications of Homogeneous Catalysis:**

1. **Fine Chemical Synthesis:** Homogeneous catalysis is widely used in the synthesis of fine chemicals, pharmaceuticals, and agrochemicals.

2. **Petrochemical Industry:** Homogeneous catalysis plays a crucial role in petroleum refining processes, such as hydrogenation, hydroformylation, and isomerization.

3. **Environmental Remediation:** Homogeneous catalysis is used in environmental applications, such as pollution control and wastewater treatment, to degrade harmful pollutants and convert them into less toxic or more easily removable forms.

Homogeneous catalysis offers significant advantages for a wide range of chemical transformations, making it a valuable tool in both industrial and academic settings.

### **Acid-base catalysis**

Acid-base catalysis is a type of catalysis in which the reaction rate is enhanced by the presence of an acid or a base. Acid-base catalysis is prevalent in a wide range of

chemical reactions, including organic, inorganic, and biochemical processes. Here's an overview of acid-base catalysis:

### **Mechanism of Acid-Base Catalysis:**

1. **Proton Transfer:** In acid-base catalysis, the catalyst (acid or base) facilitates the transfer of protons between reactants, intermediates, or transition states.
2. **Activation of Reactants:** Acid catalysis involves the donation of a proton ( $H^+$  ion) by the catalyst to one of the reactants, activating it for subsequent reaction steps. Base catalysis involves the acceptance of a proton by the catalyst from one of the reactants.
3. **Stabilization of Intermediates:** The acid or base catalyst stabilizes intermediates or transition states through electrostatic interactions or hydrogen bonding, lowering the activation energy of the reaction.

### **Types of Acid-Base Catalysis:**

1. **General Acid-Base Catalysis:** In this type of catalysis, the acid or base catalyst participates directly in the reaction by donating or accepting protons. Examples include the hydrolysis of esters and the cleavage of peptide bonds in enzymatic reactions.
2. **Specific Acid-Base Catalysis:** In specific acid-base catalysis, the acid or base catalyst interacts specifically with certain functional groups in the reactants, enhancing their reactivity. For example, strong acids catalyze the hydration of alkenes by protonating the double bond.

3. **Solvent-Mediated Acid-Base Catalysis:** Some reactions are catalyzed by acid or base species present in the reaction solvent rather than by added acids or bases. Water, for example, can act as both an acid and a base in certain reactions.

#### **Factors Influencing Acid-Base Catalysis:**

1. **Strength of the Acid or Base:** The strength of the acid or base catalyst affects its ability to donate or accept protons and thereby catalyze the reaction.
2. **Concentration of the Catalyst:** The concentration of the acid or base catalyst influences the rate of catalysis. Higher concentrations of catalyst generally lead to faster reaction rates, up to a certain point.
3. **Nature of the Substrates:** The reactivity of the substrates and the presence of functional groups that can undergo protonation or deprotonation reactions influence the effectiveness of acid-base catalysis.

#### **Applications of Acid-Base Catalysis:**

1. **Hydrolysis Reactions:** Acid-base catalysis is commonly used in the hydrolysis of esters, amides, and other functional groups in organic synthesis.
2. **Isomerization Reactions:** Acid-base catalysis plays a role in isomerization reactions, such as the isomerization of glucose to fructose in the food industry.
3. **Enzymatic Reactions:** Many enzyme-catalyzed reactions in biological systems involve acid-base catalysis, facilitating biochemical processes such as digestion, metabolism, and signal transduction.

4. **Industrial Processes:** Acid-base catalysis is employed in various industrial processes, including petroleum refining, polymerization reactions, and the production of pharmaceuticals and fine chemicals.

Acid-base catalysis is a fundamental concept in chemistry, with widespread applications in both laboratory and industrial settings. Understanding the principles and mechanisms of acid-base catalysis is essential for designing efficient synthetic routes and optimizing chemical processes.

### **Brønsted catalysis law**

The Brønsted catalysis law, also known as the Brønsted catalysis equation, describes the relationship between the reaction rate and the concentration of hydrogen ions (protons) in acid-catalyzed reactions. It is based on the principles of Brønsted-Lowry acid-base theory, which defines acids as proton donors and bases as proton acceptors. The Brønsted catalysis law provides a quantitative framework for understanding the kinetics of acid-catalyzed reactions.

### **Brønsted Catalysis Law:**

The Brønsted catalysis law can be expressed as follows:

$$\frac{d[\text{Product}]}{dt} = k \times [\text{Acid}][\text{Substrate}]$$

Where:

- $\frac{d[\text{Product}]}{dt}$  is the rate of formation of the product with respect to time,
- $k$  is the rate constant for the reaction,

- $[Acid][Acid]$  is the concentration of the acid catalyst,
- $[Substrate][Substrate]$  is the concentration of the substrate.

### Interpretation:

1. **Dependence on Acid Concentration:** The rate of the reaction is directly proportional to the concentration of the acid catalyst. This reflects the role of the acid in donating protons to activate the substrate and facilitate the reaction.
2. **Dependence on Substrate Concentration:** The rate of the reaction is also dependent on the concentration of the substrate. This reflects the frequency of collisions between the substrate molecules and the activated form of the substrate (resulting from protonation by the acid).
3. **Rate Constant  $k$ :** The rate constant  $k$  represents the intrinsic reactivity of the reaction and is influenced by factors such as temperature, solvent, and the specific chemical nature of the reaction.

### Applications:

1. **Organic Synthesis:** The Brønsted catalysis law is widely applied in organic synthesis for the design and optimization of acid-catalyzed reactions. These reactions are commonly used in the synthesis of pharmaceuticals, fine chemicals, and natural products.
2. **Petroleum Refining:** Acid-catalyzed reactions are employed in petroleum refining processes, such as hydrocracking and alkylation, to convert crude oil into valuable products like gasoline and diesel fuel.

3. **Biochemical Reactions:** Acid-catalyzed reactions play a vital role in biochemical processes such as digestion, metabolism, and signal transduction in living organisms.

4. **Material Science:** Acid-catalyzed reactions are utilized in material science for the synthesis of polymers, resins, and composite materials with tailored properties.

Understanding the Brønsted catalysis law allows chemists to predict and control the rates of acid-catalyzed reactions, enabling the development of efficient synthetic routes and the optimization of chemical processes in various fields.

### Enzyme catalysis

Enzyme catalysis is a biological process in which enzymes act as catalysts to accelerate chemical reactions within living organisms. Enzymes are specialized proteins that catalyze specific reactions by lowering the activation energy barrier, thereby increasing the rate of reaction without being consumed in the process. Enzyme catalysis is fundamental to numerous biochemical processes in living systems and plays a crucial role in metabolism, digestion, signal transduction, and other physiological functions. Here's an overview of enzyme catalysis:

#### Mechanism of Enzyme Catalysis:

1. **Substrate Binding:** Enzymes possess a specific active site where substrates bind through non-covalent interactions, such as hydrogen bonding, electrostatic interactions, and hydrophobic interactions. This binding brings the substrates into close proximity and orients them in a way that facilitates the reaction.

2. **Transition State Stabilization:** Enzymes stabilize the transition state of the reaction, which is the highest energy state along the reaction pathway. By binding to the transition state more tightly than to the substrates, enzymes lower the activation energy required for the reaction to occur.

3. **Catalytic Mechanisms:** Enzymes can employ various catalytic mechanisms to facilitate chemical reactions, including acid-base catalysis, covalent catalysis, metal ion catalysis, and proximity and orientation effects. These mechanisms involve specific amino acid residues within the enzyme's active site.

#### **Types of Enzyme Catalysis:**

1. **Hydrolase Catalysis:** Hydrolases catalyze the hydrolysis of various bonds, such as peptide bonds (proteases), glycosidic bonds (glycosidases), and ester bonds (esterases). These enzymes typically use water molecules as nucleophiles to cleave the substrate.

2. **Oxidoreductase Catalysis:** Oxidoreductases catalyze oxidation-reduction reactions by transferring electrons between substrates. Examples include dehydrogenases, which transfer hydride ions ( $H^-$ ) or hydrogen atoms ( $H^+$ ), and oxidases, which transfer oxygen atoms or electrons to molecular oxygen.

3. **Transferase Catalysis:** Transferases catalyze the transfer of functional groups, such as methyl, acyl, or phosphoryl groups, between substrates. Examples include kinases, which transfer phosphate groups, and transaminases, which transfer amino groups.

4. **Isomerase Catalysis:** Isomerases catalyze the interconversion of isomers, including structural isomers, stereoisomers, and geometric isomers. Examples include racemases, which catalyze the racemization of chiral compounds, and cis-trans isomerases, which catalyze the cis-trans isomerization of double bonds.

### Factors Affecting Enzyme Catalysis:

1. **Substrate Concentration:** Increasing substrate concentration generally increases the rate of enzyme catalysis until the enzyme becomes saturated with substrate ( $V_{max}$ ).
2. **Enzyme Concentration:** Higher enzyme concentrations typically lead to faster reaction rates, assuming substrate concentration is not limiting.
3. **pH and Temperature:** Enzyme activity is influenced by pH and temperature, with each enzyme exhibiting an optimal pH and temperature range for catalytic activity.
4. **Cofactors and Coenzymes:** Many enzymes require non-protein cofactors or coenzymes for catalytic activity. These molecules assist in enzyme-substrate binding or participate directly in catalytic mechanisms.

### Applications of Enzyme Catalysis:

1. **Biotechnology:** Enzymes are widely used in biotechnological applications, including enzyme assays, protein engineering, and the production of pharmaceuticals, biofuels, and food additives.
2. **Diagnostics:** Enzymes are utilized in diagnostic assays and kits for detecting biomarkers, pathogens, and genetic mutations in clinical and research laboratories.
3. **Bioremediation:** Enzymes play a role in bioremediation processes for the degradation of environmental pollutants, such as oil spills, pesticides, and industrial chemicals.



4. **Food Industry:** Enzymes are used in food processing and production for various purposes, including dough conditioning, cheese production, brewing, and fruit juice clarification.

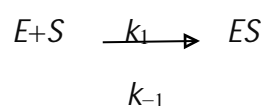
Enzyme catalysis is a fundamental process in biology with diverse applications in biotechnology, medicine, industry, and environmental science. Understanding the mechanisms and regulation of enzyme catalysis is essential for advancing our knowledge of biochemical processes and developing innovative solutions to complex challenges.

### Michelis-Menton catalysis

The Michaelis-Menten equation describes the rate of an enzyme-catalyzed reaction as a function of substrate concentration. It is derived under certain assumptions, which include the formation of an enzyme-substrate complex and the steady-state approximation. Here, the derivation of the Michaelis-Menten equation in all its cases:

#### Case 1: Formation of Enzyme-Substrate Complex (ES):

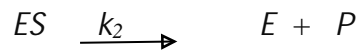
##### 1. Step 1 - Formation of ES Complex:



- $E$  represents free enzyme,
- $S$  represents substrate,
- $ES$  represents enzyme-substrate complex,
- $k_1$  is the forward rate constant for ES complex formation,
- $k_{-1}$  is the backward rate constant for ES complex dissociation.

## Case 2: Formation of Product (P):

### 2. Step 2 - Formation of Product:



- $\rightarrow k_2$  is the rate constant for product formation.

### Assumptions:

- The formation of ES complex is rapid compared to its breakdown ( $k_1 \gg k_{-1}$ ).
- The ES complex reaches a steady-state concentration, meaning the rate of formation of ES equals its breakdown ( $d[ES]/dt = 0$ ).

### Derivation:

#### 1. Rate of Formation of ES:

$$d[ES]/dt = k_1[E][S] - k_{-1}[ES]$$

#### 2. At Steady State:

$$0 = k_1[E][S] - k_{-1}[ES]$$

$$[ES] = \frac{k_1}{k_{-1}}[E][S]$$

#### 3. Total Enzyme Concentration:

$$[E]_{\text{total}} = [E] + [ES]$$

$$[E]_{\text{total}} = [E] + \frac{k_1}{k_{-1}}[E][S]$$

$$[E]_{\text{total}} = [E](1 + K_m[S])$$

Where

$K_m = \frac{k_{-1}}{k_1 + k_2}$  is the Michaelis constant.

#### 4. Rate of Reaction:

$$\text{Rate} = k_2[ES]$$

$$\text{Rate} = \frac{k_1 k_2 [E][S]}{k_1 + k_2 [S]}$$

$$\text{Rate} = \frac{k_2 [E]_{\text{total}} [S]}{K_m + [S]}$$

$$\text{Rate} = \frac{V_{\text{max}} [S]}{K_m + [S]}$$

Where total  $V_{\text{max}} = k_2 [E]_{\text{total}}$  is the maximum reaction rate.

#### Michaelis-Menten Equation:

$$\text{Rate} = \frac{V_{\text{max}} [S]}{K_m + [S]}$$

Cases:

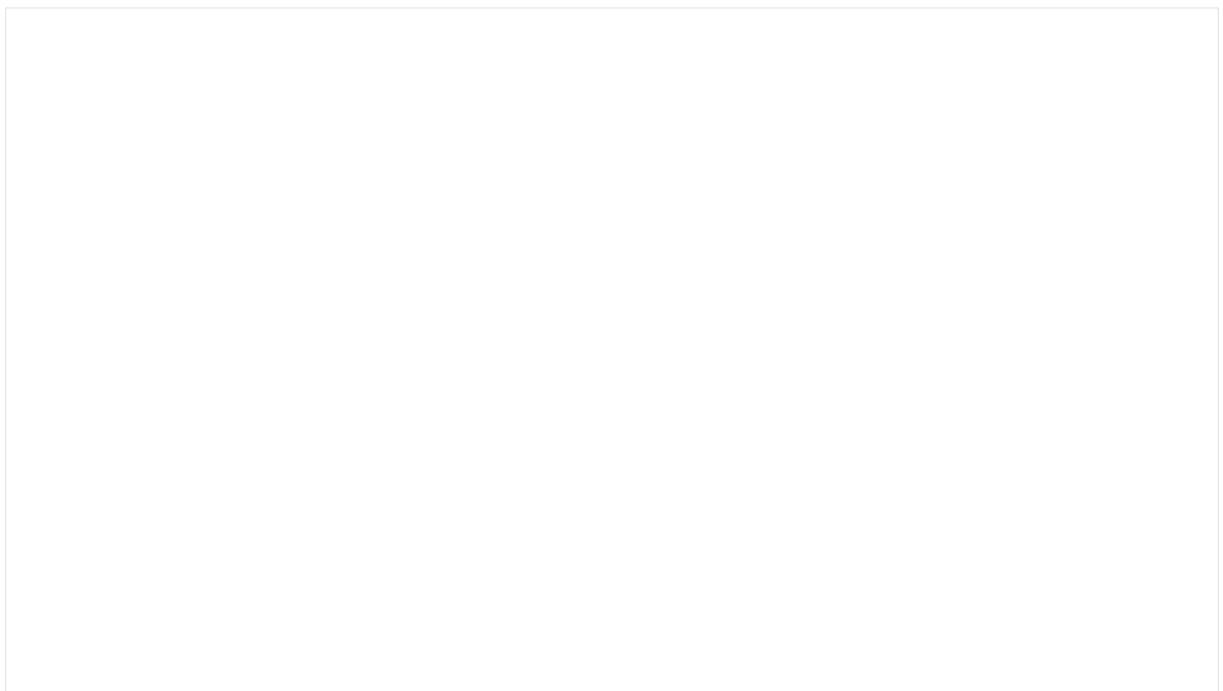
##### 1. When $[S] \ll K_m$ (Low Substrate Concentration):

- The rate of reaction is approximately linear with respect to substrate concentration  $\text{Rate} \approx \frac{V_{\text{max}}}{K_m} [S]$ .

##### 2. When $[S] \gg K_m$ (High Substrate Concentration):

- The rate of reaction approaches the maximum velocity ( $V_{\text{max}}$ ), as the enzyme is saturated with substrate.

The Michaelis-Menten equation provides a fundamental framework for understanding enzyme kinetics and is widely used in biochemistry and enzymology to analyze enzyme-catalyzed reactions.



## UNIT-V

### Kinetics of Fast and Complex Reactions

#### Complex Reactions

##### Reversible reaction

In a reversible process, if the rate of backward reaction is much less as compared to the rate of forward reaction, the equilibrium will be far away from the starting end and the reaction may be found to follow a simple and straightforward path as discussed earlier. However, when the reaction rates are appreciable for both the forward and backward directions, the kinetics must be taken into consideration for both the direction.

The kinetics of fast reversible reactions are characterized by their rapid rates of forward and backward reactions, where reactants are quickly converted into products and vice versa. In such reactions, the forward and backward reactions are nearly in equilibrium, meaning that the concentrations of both reactants and products remain relatively constant over time.

The rate of a reversible reaction can be described by the rate law, which typically includes rate constants for both the forward and backward reactions. The rate of the forward reaction ( $\text{rate}_f$ ) and the rate of the backward reaction ( $\text{rate}_b$ ) are related to the concentrations of reactants and products according to the following equations, which are based on the law of mass action:

$$\text{rate}_f = k_f \times [\text{reactants}]$$

$$\text{rate}_b = k_b \times [\text{products}]$$

Where:

- $k_f$  is the rate constant for the forward reaction.
- $k_b$  is the rate constant for the backward reaction.
- $[\text{reactants}]$  and  $[\text{products}]$  are the concentrations of the reactants and products, respectively.

For fast reversible reactions, the rate constants  $k_f$  and  $k_b$  are typically high, indicating rapid interconversion between reactants and products.

The equilibrium constant ( $K_{eq}$ ) for the reaction is defined as the ratio of the rate constants for the forward and backward reactions:

$$K_{eq} = \frac{k_f}{k_b}$$

At equilibrium, the forward and backward rates are equal, so the rate of the forward reaction equals the rate of the backward reaction:

$$\text{rate}_f = \text{rate}_b$$

$$k_f \times [\text{reactants}] = k_b \times [\text{products}]$$

From this equation, we can derive the expression for the equilibrium constant:

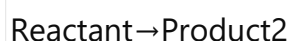
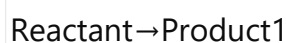
$$K_{eq} = \frac{[\text{products}]}{[\text{reactants}]}$$

The kinetics of fast reversible reactions involve rapid interconversion between reactants and products, with equilibrium reached relatively quickly. The concentrations of reactants and products remain relatively stable at equilibrium, determined by the equilibrium constant.

## Parallel reactions

When a reactant in the reaction undergoes in more than one pathway giving rise to different products, the reactions are termed as parallel or side reactions. Parallel reactions occur when multiple reactions can proceed simultaneously, leading to the formation of different products from the same reactants. The kinetics of parallel reactions can be described using the rate laws for each individual reaction involved.

Let's consider a simple case of two parallel reactions:



The rate of each reaction ( $\text{rate}_1$  and  $\text{rate}_2$ ) can be described by their respective rate laws:

$$\text{rate}_1 = k_1 \times [\text{Reactant}]$$

$$\text{rate}_2 = k_2 \times [\text{Reactant}]$$

Where:

- $k_1$  and  $k_2$  are the rate constants for reactions 1 and 2, respectively.
- $[\text{Reactant}]$  is the concentration of the reactant.

The overall rate of reaction ( $\text{rate}_{\text{overall}}$ ) is the sum of the rates of the individual reactions:

$$\text{rate}_{\text{overall}} = \text{rate}_1 + \text{rate}_2$$

$$\text{rate}_{\text{overall}} = \text{rate}_1 + \text{rate}_2$$

At any given time, the change in the concentration of the reactant is given by the negative of the overall rate:

$$d[\text{Reactant}]/dt = -\text{rate}_{\text{overall}}$$

The change in the concentration of each product is given by the rate of its respective reaction:

$$d[\text{Product1}]/dt = \text{rate1}$$

$$d[\text{Product2}]/dt = \text{rate2}$$

These differential equations can be solved to determine the concentrations of reactants and products as a function of time.

The kinetics of parallel reactions involve the consideration of multiple reactions occurring simultaneously, each with its own rate constant and rate law. The overall rate of reaction is the sum of the rates of the individual reactions.

### **Consecutive reactions**

Consecutive reactions, also known as sequential reactions, occur when multiple reactions proceed in sequence, where the product of one reaction becomes the reactant of the subsequent reaction. The kinetics of consecutive reactions can be described using a series of rate laws for each individual step.

Let's consider a simple case of two consecutive reactions:

1. Reactant  $\rightarrow$  Intermediate
2. Intermediate  $\rightarrow$  Product



The rate of each reaction (rate<sub>1</sub> and rate<sub>2</sub>) can be described by their respective rate laws:

$$\text{rate}_1 = k_1 \times [\text{Reactant}]$$

$$\text{rate}_2 = k_2 \times [\text{Intermediate}]$$

Where:

- $k_1$  and  $k_2$  are the rate constants for reactions 1 and 2, respectively.
- $[\text{Reactant}]$  is the concentration of the reactant.
- $[\text{Intermediate}]$  is the concentration of the intermediate formed in the first reaction.

The overall rate of the consecutive reactions depends on the slowest step, which in this case is the second reaction. Therefore, the overall rate of reaction is given by the rate of the second reaction:

$$\text{rate}_{\text{overall}} = \text{rate}_2$$

$$\text{rate}_{\text{overall}} = \text{rate}_2$$

At any given time, the change in the concentration of the reactant and intermediate are given by the negative of the overall rates of their respective reactions:

$$d[\text{Reactant}] / dt = -\text{rate}_1$$

$$d[\text{Intermediate}] / dt = -\text{rate}_1 + \text{rate}_2$$

The change in the concentration of the product is given by the rate of the second reaction:

$$d[\text{Product}] / dt = \text{rate}_2$$

These differential equations can be solved to determine the concentrations of reactants, intermediates, and products as a function of time.

The kinetics of consecutive reactions involve multiple reactions proceeding in sequence, with the overall rate determined by the slowest step. Each step contributes to the overall rate, and the concentrations of reactants, intermediates, and products change over time according to their respective rate laws.

### Chain reactions

Chain reactions are complex processes where a series of reactions occur in a self-propagating manner, typically involving the generation of reactive intermediates that initiate further reactions. These reactions can be categorized into three main steps: initiation, propagation, and termination.

1. **Initiation:** In this step, a reactive species, often referred to as an initiator, is formed. This can occur through various means such as thermal decomposition, photolysis, or reaction with another molecule.
2. **Propagation:** Once the initiator is formed, it reacts with other molecules to generate reactive intermediates. These intermediates then react with additional molecules, continuing the chain of reactions. The propagation steps repeat until termination occurs.
3. **Termination:** Termination steps involve the destruction of reactive intermediates, typically by their reaction with each other or with another molecule in the system. Termination steps ultimately lead to the cessation of the chain reaction.

The kinetics of chain reactions are highly dependent on the specific mechanism and conditions of the reaction. However, some general features can be outlined:

- **Rate of initiation:** The rate of initiation determines how quickly the chain reaction begins. It is often dependent on factors such as temperature, concentration of reactants, and the presence of catalysts.
- 
- **Rate of propagation:** The rate of propagation is determined by the concentration of reactive intermediates and the rate constants for their reactions with other species. This step is typically the fastest in the chain reaction process.
- 
- **Rate of termination:** The rate of termination determines how quickly the chain reaction is terminated. It is influenced by the concentration of reactive intermediates and the probability of their collision with each other or other molecules leading to termination.

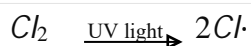
The overall rate of a chain reaction depends on the balance between initiation, propagation, and termination steps. If initiation and propagation dominate over termination, the chain reaction can proceed rapidly and potentially explosively. Conversely, if termination predominates, the chain reaction will be slow or may not sustain itself over time.

Mathematically describing the kinetics of chain reactions often involves complex kinetic models and mechanisms, including differential equations that account for the concentrations of various species involved in each step of the reaction. These models may also incorporate factors such as branching reactions, where one reactive intermediate can generate multiple new intermediates, further complicating the kinetics of the chain reaction.

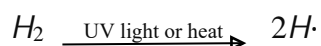
## Kinetics of the reaction between $H_2 - Cl_2$

The reaction between hydrogen gas ( $H_2$ ) and chlorine gas ( $Cl_2$ ) is a well-known example of a chain reaction, specifically a radical chain reaction. This reaction proceeds through several steps, including initiation, propagation, and termination.

1. **Initiation:** The reaction can be initiated by various means, such as exposure to ultraviolet (UV) light or thermal energy. For example, under UV light, chlorine molecules dissociate into two chlorine radicals ( $Cl\cdot$ ):



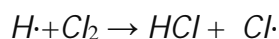
Similarly, hydrogen gas can also undergo homolytic cleavage to form two hydrogen radicals ( $H\cdot$ ):



2. **Propagation:** Once the radicals are formed, they can react with molecules of the other reactant to form new radicals and products. For instance, a chlorine radical can react with a hydrogen molecule to form hydrogen chloride ( $HCl$ ) and another hydrogen radical:

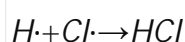
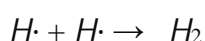


The newly formed hydrogen radical can then react with a chlorine molecule to form another molecule of hydrogen chloride and regenerate the chlorine radical:



These propagation steps continue, with the radicals generated in one step initiating further reactions in subsequent steps, thus propagating the chain reaction.

3. **Termination:** The chain reaction can be terminated when radicals react with each other or with stable molecules to form non-radical products. For example:



These termination steps remove radicals from the system, ultimately slowing down or stopping the chain reaction.

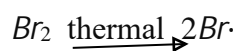
The kinetics of the  $H_2$ - $Cl_2$  reaction involve understanding the rates of initiation, propagation, and termination steps. The overall rate of the reaction is determined by the balance between these steps. Typically, the propagation steps dominate the kinetics of the reaction, as they involve the formation of products and the regeneration of radicals, which sustain the chain reaction.

### **Kinetics of the reaction between $H_2$ – $Br_2$**

The reaction between hydrogen gas ( $H_2$ ) and bromine gas ( $Br_2$ ) can proceed via both thermal and photochemical pathways. Let's explore both pathways and discuss their chain lengths.

#### **Thermal Reaction:**

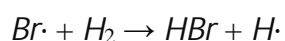
1. **Initiation:** In the thermal reaction, the initiation step involves the breaking of the  $Br_2$  molecule to form bromine radicals ( $Br\cdot$ ).



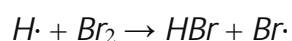
Similarly, hydrogen gas can undergo homolytic cleavage to form hydrogen radicals ( $H\cdot$ ).



2. **Propagation:** The bromine radicals react with hydrogen gas to form hydrogen bromide ( $HBr$ ) and another hydrogen radical.



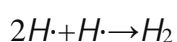
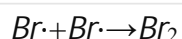
The newly formed hydrogen radical can then react with a bromine molecule to form another molecule of hydrogen bromide and regenerate the bromine radical.

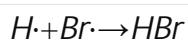


These propagation steps continue, sustaining the chain reaction.

3. **Termination:** The chain reaction terminates when radicals react with each other or with stable molecules to form non-radical products. For example:

4.





### Photochemical Reaction:

In the photochemical reaction, the initiation step involves the absorption of UV light by the  $Br_2$  molecule to form bromine radicals ( $Br\cdot$ ).



The propagation and termination steps are the same as those in the thermal reaction.

### Chain Length:

The chain length of a chain reaction refers to the average number of propagation steps that occur before termination. In both the thermal and photochemical reactions of  $H_2-Br_2$ , the chain length can vary depending on factors such as temperature, pressure, and the presence of inhibitors or catalysts.

In general, for the thermal reaction, the chain length tends to be shorter compared to the photochemical reaction. This is because the thermal reaction typically requires higher temperatures to initiate, and at these temperatures, termination reactions may occur more frequently, leading to a shorter chain length.

In contrast, the photochemical reaction can initiate at lower temperatures, and the initiation step produces highly reactive radicals, which can sustain longer chains before termination occurs. Therefore, the chain length of the photochemical reaction is generally longer compared to the thermal reaction.

Overall, the chain length of the  $H_2-Br_2$  reaction can be influenced by various factors and is determined by the balance between the rates of initiation, propagation, and termination steps.

## Rice-Herzfeld mechanism

The Rice-Herzfeld mechanism, also known as the Rice-Herzfeld chain branching mechanism, describes a type of chain reaction mechanism often observed in gas-phase reactions involving halogen atoms. This mechanism was proposed by Rice and Herzfeld in 1924 and has been used to explain various reactions involving halogen radicals, such as the reactions of hydrogen with halogens (e.g.,  $H_2-Cl_2$ ,  $H_2-Br_2$ ).

The Rice-Herzfeld mechanism consists of three main steps: initiation, propagation, and termination.

### 1. Initiation:

- The initiation step involves the generation of radical species, typically through the input of energy, such as heat or light.

For example, in the  $H_2-Cl_2$  reaction: ·



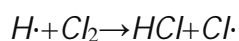
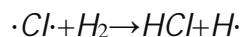
- These radicals are highly reactive and serve as the initiators of the chain reaction.
- 

### 2. Propagation:

- In the propagation step, the radicals react with the reactant molecules to form new radicals and products, thereby propagating the chain reaction.



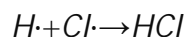
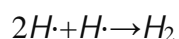
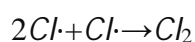
- For example, in the H<sub>2</sub>-Cl<sub>2</sub> reaction:



- The newly formed radicals continue to react with additional reactant molecules, leading to the generation of more radicals and products.
- The propagation steps continue in a chain-like fashion, resulting in the sustained reaction of reactants to form products.
- 

### 3. Termination:

- The termination steps involve the destruction of radicals, typically by their reaction with each other or with stable molecules, leading to the cessation of the chain reaction.
- For example:



- These termination steps remove radicals from the system, ultimately slowing down or stopping the chain reaction.

The Rice-Herzfeld mechanism accounts for the branching nature of the chain reaction, where one radical can produce multiple new radicals through the

propagation steps, leading to exponential growth in the number of radicals and the rate of reaction.

Overall, the Rice-Herzfeld mechanism provides a framework for understanding the behavior of chain reactions involving radical species and has been widely used to elucidate the kinetics and mechanisms of various gas-phase reactions, particularly those involving halogen radicals.

### **Kinetics of Free radical polymerization**

Free radical polymerization is a widely used method for synthesizing polymers, where monomers are polymerized in the presence of radical initiators. The kinetics of free radical polymerization involve several steps, including initiation, propagation, and termination.

#### **1. Initiation:**

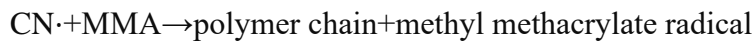
- The initiation step involves the generation of free radicals, typically through the decomposition of a radical initiator. Common radical initiators include azo compounds (e.g., azobisisobutyronitrile, AIBN) and peroxides (e.g., benzoyl peroxide).
- For example, with AIBN as the initiator:
- 



- These radicals initiate the polymerization process by attacking the double bond of a monomer to form a new radical species.

#### **2. Propagation:**

- In the propagation step, the radicals react with monomer molecules, leading to the growth of polymer chains. This step involves the addition of monomer units to the growing polymer chain.
- For example, with methyl methacrylate (MMA) as the monomer:

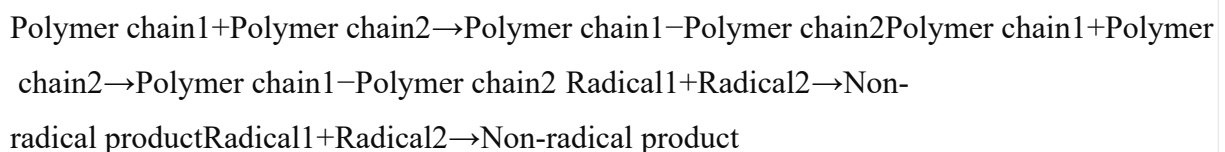


- The newly formed radical can then react with another monomer molecule, continuing the chain growth process.

### 3. Termination:

- Termination steps occur when radicals combine to form non-radical species, thus stopping the chain growth. There are several termination pathways:
  - Combination termination: Two growing polymer chains combine.
  - Disproportionation termination: One polymer chain donates a hydrogen atom to another polymer chain, resulting in two polymer chains of different lengths.
  - Radical-radical termination: Two radicals combine to form a non-radical species.

- For example:



### Rate Equations:

- The rate of polymerization ( $R_p$ ) can be expressed in terms of the concentration of radicals and monomers, the rate constants for initiation and propagation, and the degree of polymerization.
- Typically, the rate of polymerization is proportional to the square root of the initiator concentration and the concentration of monomer.

- The overall kinetics of free radical polymerization can be complex due to factors such as termination reactions, transfer reactions, and the presence of inhibitors or chain transfer agents.

### **Chain Length Distribution:**

- Free radical polymerization often leads to a distribution of polymer chain lengths due to termination and transfer reactions. This distribution can be characterized by methods such as gel permeation chromatography (GPC).

Understanding the kinetics of free radical polymerization is crucial for controlling polymerization processes and designing polymers with desired properties. Kinetic modeling and experimental techniques are used to study and optimize polymerization reactions in various industrial and academic applications

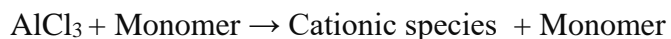
### **Kinetics of Cationic polymerization**

Cationic polymerization is a type of chain-growth polymerization where monomers react with cationic initiators to form polymer chains. The kinetics of cationic polymerization differ from those of free radical polymerization and are influenced by factors such as the nature of the monomer, initiator, solvent, and temperature. Here's an overview of the kinetics of cationic polymerization:

#### **1. Initiation:**

- Cationic polymerization typically begins with the generation of a cationic species, often through the action of a Lewis acid or a protic acid. Common initiators include Lewis acids such as aluminum chloride ( $AlCl_3$ ) or protic acids such as sulfuric acid ( $H_2SO_4$ ).

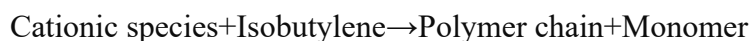
- For example, with aluminum chloride as the initiator:



- The generated cationic species can then initiate the polymerization by attacking the double bond of the monomer to form a reactive intermediate.

## 2. Propagation:

- In the propagation step, the cationic species reacts with monomer molecules to extend the polymer chain. This step involves the addition of monomer units to the growing polymer chain.
- For example, with isobutylene (a monomer) and a cationic species:



- 
- The reactive intermediate formed continues to react with monomer molecules, leading to the growth of the polymer chain.

## 3. Termination:

- Termination steps can occur through various mechanisms, including the combination of active species or the reaction with impurities or inhibitors.
- Termination reactions result in the cessation of chain growth and the formation of non-reactive species.
- For example:  $\text{Cationic species}_1 + \text{Cationic species}_2 \rightarrow \text{Non-reactive product}$

## Rate Equations:

- The rate of cationic polymerization is influenced by factors such as the concentration of initiators, monomers, and solvents, as well as temperature.

- Kinetic modeling of cationic polymerization often involves complex rate equations that consider the concentrations of active species, monomers, and inhibitors, as well as the rates of initiation, propagation, and termination.

### **Chain Length Distribution:**

- Cationic polymerization typically results in relatively narrow molecular weight distributions compared to free radical polymerization.
- The control of chain length distribution in cationic polymerization is crucial for achieving desired polymer properties and applications.

Understanding the kinetics of cationic polymerization is essential for optimizing polymerization conditions, controlling molecular weight, and designing polymers with specific properties for various industrial and academic applications. Kinetic studies and experimental techniques are employed to elucidate the mechanisms and kinetics of cationic polymerization reactions

### **Kinetics of Anionic polymerization**

Anionic polymerization is a type of chain-growth polymerization where monomers react with anionic initiators to form polymer chains. The kinetics of anionic polymerization are different from those of free radical and cationic polymerization and are characterized by specific rate equations. Here's an overview of the kinetics of anionic polymerization, including the relevant rate equations:

#### **1. Initiation:**

- Anionic polymerization typically begins with the generation of anionic species, often through the action of strong bases such as alkyl lithium or alkyl magnesium compounds.
- For example, with butyllithium (*BuLi*) as the initiator:



- The generated anionic species can then initiate the polymerization by attacking the monomer to form a reactive intermediate.

## 2. Propagation:

- In the propagation step, the anionic species reacts with monomer molecules to extend the polymer chain. This step involves the addition of monomer units to the growing polymer chain.
- For example, with styrene (a monomer) and an anionic species:  

$$\text{Anionic species} + \text{Styrene} \rightarrow \text{Polymer chain} + \text{Monomer}$$

$$\text{Anionic species} + \text{Styrene} \rightarrow \text{Polymer chain} + \text{Monomer}$$
- The reactive intermediate formed continues to react with monomer molecules, leading to the growth of the polymer chain.

## 3. Termination:

- Termination steps in anionic polymerization can occur through various mechanisms, including the combination of active species or the reaction with impurities or terminators.
- Termination reactions result in the cessation of chain growth and the formation of non-reactive species.
- For example:  $\text{Anionic species}_1 + \text{Anionic species}_2 \rightarrow \text{Non-reactive product}$   

$$\text{Anionic species}_1 + \text{Anionic species}_2 \rightarrow \text{Non-reactive product}$$

### Rate Equations:

- The rate of anionic polymerization is influenced by factors such as the concentration of initiators, monomers, and solvents, as well as temperature.
- Kinetic modeling of anionic polymerization often involves complex rate equations that consider the concentrations of active species, monomers, and inhibitors, as well as the rates of initiation, propagation, and termination.
- The rate of propagation ( $R_p$ ) in anionic polymerization is typically proportional to the concentration of monomer and the concentration of the anionic species.

$$R_p = k_p \times [\text{Monomer}] \times [\text{Anionic species}]$$

- The rate of termination depends on the concentration of active species and can involve various termination mechanisms.

- The overall rate equation for anionic polymerization can be written as:
- 

$$d[P]/dt = k_i \times [\text{Initiator}] - k_t \times [\text{Active species}] \times [\text{Monomer}]^2$$

### Chain Length Distribution:

- Anionic polymerization typically results in relatively narrow molecular weight distributions compared to free radical polymerization.
- The control of chain length distribution in anionic polymerization is crucial for achieving desired polymer properties and applications.

Understanding the kinetics of anionic polymerization is essential for optimizing polymerization conditions, controlling molecular weight, and designing polymers with specific properties for various industrial and academic applications. Kinetic



studies and experimental techniques are employed to elucidate the mechanisms and kinetics of anionic polymerization reactions.

## Kinetics of Polycondensation polymerization

Polycondensation polymerization involves the reaction of multifunctional monomers, typically containing two or more reactive groups, to form polymer chains with the elimination of small molecules such as water, alcohol, or hydrogen chloride. The kinetics of polycondensation polymerization can be complex due to the simultaneous occurrence of multiple reaction steps, including condensation, addition, and elimination reactions. Here's an overview of the kinetics of polycondensation polymerization, including the relevant rate equations:

### 1. Initiation:

- Polycondensation polymerization often does not involve a separate initiation step as in other types of polymerization. Instead, it begins with the reaction of multifunctional monomers.

### 2. Propagation:

- In polycondensation polymerization, propagation occurs through the repetitive reaction of monomer units, resulting in the formation of polymer chains.
- The rate of propagation depends on the concentration of reactive functional groups on the monomers and the degree of polymerization.
- The rate of propagation ( $R_p$ ) can be expressed as:
- $R_p = k_p \times [\text{Monomer}]^n \times [\text{Polymer chain}]^m$

- $k_p$  is the rate constant for propagation.

- $n$  and  $m$  are the stoichiometric coefficients of the monomer and the polymer chain in the reaction.

### 3. Termination:

- Termination steps in polycondensation polymerization involve the combination of reactive end groups or the reaction with impurities or terminators.
- Termination reactions result in the cessation of chain growth and the formation of non-reactive species.
- For example:  $\text{Polymer chain}_1 + \text{Polymer chain}_2 \rightarrow \text{Non-reactive product}$

### 4. Equilibrium Reactions:

- In polycondensation polymerization, equilibrium reactions may occur between the polymer chains and the small molecules released during polymerization (e.g., water, alcohol).
- These equilibrium reactions influence the kinetics and the extent of polymerization.
- The equilibrium constant for such reactions can be expressed using the law of mass action.

### Rate Equations:

- The overall rate of polycondensation polymerization depends on the rates of propagation, termination, and any equilibrium reactions.
- Kinetic modeling of polycondensation polymerization often involves complex rate equations that consider the concentrations of monomers, polymer chains, small molecules, and any catalysts or inhibitors present.

- The rate equation for polycondensation polymerization may vary depending on the specific monomers and reaction conditions involved.

### **Chain Length Distribution:**

- Polycondensation polymerization typically results in a broad distribution of polymer chain lengths due to the simultaneous occurrence of propagation and termination reactions.
- The distribution of chain lengths influences the properties of the resulting polymer.

Understanding the kinetics of polycondensation polymerization is essential for optimizing reaction conditions, controlling molecular weight distribution, and designing polymers with specific properties for various industrial and academic applications. Kinetic studies and experimental techniques are employed to elucidate the mechanisms and kinetics of polycondensation polymerization reactions.

### **Fast Reactions**

One of the important recent developments in chemical kinetics has been a great interest in the study of very fast reactions which complete in less than about 1 sec. With special laser techniques it is now possible to study the reactions occurring in a few pico seconds ( $\approx 10^{-12}$ sec). The techniques, which have been designed to monitor concentrations and to measure the rate coefficients, include flash photolysis, relaxation methods and flow techniques. The other techniques including shock tubes and molecular beams have been used to explore the dependence of reaction rate on the state of rotational/ vibrational excitation of molecules or on the energy with

which molecules collide and the rate (state-to-state cross sections and rates) at which the energy is changed from one form into another.

### Ranges of rate constants amenable to different techniques

Technique	Range of rate constant
Conventional methods	$10^{-7} \text{ s}^{-1}$ to $1 \text{ s}^{-1}$ ; $10^{-7} \text{ mol}^{-1}\text{dm}^3\text{s}^{-1}$ to $1 \text{ mol}^{-1}\text{dm}^3\text{s}^{-1}$
Rapid reaction methods	$1 \text{ s}^{-1}$ to $10^9 \text{ s}^{-1}$ ; $1 \text{ mol}^{-1}\text{dm}^3\text{s}^{-1}$ to $10^{11} \text{ mol}^{-1}\text{dm}^3\text{s}^{-1}$
<b>Flow methods</b>	$10^2$ - $10^8 \text{ mol}^{-1}\text{dm}^3\text{s}^{-1}$
Continuous flow method	$10^2$ - $10^7 \text{ mol}^{-1}\text{dm}^3\text{s}^{-1}$
Accelerated flow method	$10^2$ - $10^8 \text{ mol}^{-1}\text{dm}^3\text{s}^{-1}$
Stopped flow method	$10^2$ - $10^8 \text{ mol}^{-1}\text{dm}^3\text{s}^{-1}$
<b>Relaxation method</b>	$10^2$ - $10^{11} \text{ mol}^{-1}\text{dm}^3\text{s}^{-1}$

Temperature jump	$10^2$ - $10^3$ mol <sup>-1</sup> dm <sup>3</sup> s <sup>-1</sup>
Pressure jump	$10^2$ - $10^{11}$ mol <sup>-1</sup> dm <sup>3</sup> s <sup>-1</sup>
Electric impulse	$10^4$ - $10^{11}$ mol <sup>-1</sup> dm <sup>3</sup> s <sup>-1</sup>
Ultrasonic	
Initiating of the reaction by radiation flash photolysis	$10^2$ - $10^{10}$ mol <sup>-1</sup> dm <sup>3</sup> s <sup>-1</sup>
Magnetic resonance spectroscopy	$10^5$ - $10^{11}$ mol <sup>-1</sup> dm <sup>3</sup> s <sup>-1</sup>  $10^2$ - $10^{11}$ mol <sup>-1</sup> dm <sup>3</sup> s <sup>-1</sup>
Electron spin resonance	
Nuclear magnetic resonance	

### Study of fast reactions

In the study of fast reactions, relaxation methods are experimental techniques used to investigate the kinetics and mechanism of reactions that occur on short timescales. These methods are particularly useful for studying reactions with rapid kinetics, where traditional methods may not provide sufficient temporal resolution.

Relaxation methods typically involve inducing a sudden change in reaction conditions, such as temperature, pressure, or concentration, and monitoring the subsequent relaxation of the system as it returns to equilibrium. The relaxation of the system provides valuable information about reaction rates, reaction mechanisms, and the nature of intermediates involved.

There are several relaxation methods commonly used in the study of fast reactions:

### **1. Temperature Jump (T-jump) Relaxation:**

- In T-jump relaxation experiments, the temperature of the reaction mixture is rapidly increased or decreased using a laser pulse or an electric heating element.
- The subsequent relaxation of the system is monitored using spectroscopic techniques such as infrared spectroscopy or fluorescence spectroscopy.
- T-jump relaxation experiments are particularly useful for studying the kinetics of chemical reactions that are temperature-sensitive.

### **2. Pressure Jump Relaxation:**

- Pressure jump relaxation experiments involve the sudden change in pressure of the reaction mixture using techniques such as rapid compression or expansion.
- The relaxation of the system is monitored using techniques such as spectroscopy or mass spectrometry.
- Pressure jump relaxation experiments are useful for studying reactions involving gas-phase species or reactions influenced by changes in pressure.

### **3. pH Jump Relaxation:**

- pH jump relaxation experiments involve the sudden change in pH of the reaction mixture by adding acid or base.
- The subsequent relaxation of the system is monitored using techniques such as pH measurement, spectroscopy, or chromatography.
- pH jump relaxation experiments are useful for studying reactions involving proton transfer or acid-base catalysis.

### **4. Concentration Jump Relaxation:**

- Concentration jump relaxation experiments involve the rapid mixing of reactants or addition of a chemical species to induce a sudden change in concentration.
- The relaxation of the system is monitored using techniques such as spectroscopy, chromatography, or electrochemistry.
- Concentration jump relaxation experiments are useful for studying reactions involving fast chemical equilibria or complex reaction mechanisms.

### **5. Optical Pump-Probe Spectroscopy:**

- Optical pump-probe spectroscopy involves the excitation of a sample with an intense laser pulse (pump) followed by the measurement of changes in optical properties (probe) over time.
- This technique provides information about the dynamics of excited states, molecular rearrangements, and reaction kinetics.
- Optical pump-probe spectroscopy is widely used for studying ultrafast processes in both chemical and biological systems.

Relaxation methods offer a powerful approach for studying the kinetics and mechanism of fast reactions, providing valuable insights into reaction pathways, transient intermediates, and reaction rates. These techniques have applications in various fields, including chemical kinetics, biophysics, and materials science.

Electric and magnetic field jump methods are experimental techniques used to study the kinetics and dynamics of reactions involving charged species, such as ions or polar molecules. These methods involve the sudden change in the strength or orientation of electric or magnetic fields applied to the reaction mixture, followed by the monitoring of the subsequent relaxation of the system. Here's an overview of these methods along with diagrams illustrating their principles:

#### **Electric Field Jump Method:**

#### **Principle:**

- In the electric field jump method, a sudden change in the strength of an applied electric field is used to perturb the orientation and behavior of charged species in the reaction mixture.
- The electric field affects the mobility, orientation, and reactivity of charged species, influencing the kinetics and mechanism of reactions involving charged intermediates.

#### **Experimental Setup:**

- A typical experimental setup for electric field jump experiments involves two parallel electrodes immersed in the reaction mixture. The electrodes are connected to a power source capable of generating a high-voltage electric field.
- The reaction mixture contains charged species or polar molecules that can interact with the electric field.

#### **Procedure:**

1. Initially, the reaction mixture is in a state of equilibrium or steady-state conditions.
2. A high-voltage electric field is suddenly applied across the electrodes, causing a rapid change in the strength of the electric field in the reaction mixture.
3. The reaction kinetics and dynamics are monitored using spectroscopic techniques, such as time-resolved fluorescence or absorption spectroscopy, to observe changes in the concentration or behavior of reactive intermediates.

#### **Magnetic Field Jump Method:**

##### **Principle:**

- In the magnetic field jump method, a sudden change in the orientation or strength of an applied magnetic field is used to influence the alignment and behavior of paramagnetic species in the reaction mixture.
- The magnetic field affects the orientation, spin dynamics, and reactivity of paramagnetic species, providing insights into their role in reaction mechanisms.



### **Experimental Setup:**

- A typical experimental setup for magnetic field jump experiments involves the use of a pair of Helmholtz coils to generate a uniform magnetic field perpendicular to the reaction mixture.
- The reaction mixture contains paramagnetic species or molecules with unpaired electrons that can interact with the magnetic field.

### **Procedure:**

1. Initially, the reaction mixture is in a state of equilibrium or steady-state conditions.
2. A sudden change in the orientation or strength of the magnetic field is induced by modulating the current passing through the Helmholtz coils.
3. The reaction kinetics and dynamics are monitored using spectroscopic techniques, such as electron paramagnetic resonance (EPR) spectroscopy or nuclear magnetic resonance (NMR) spectroscopy, to observe changes in the concentration or behavior of paramagnetic species.

These electric and magnetic field jump methods offer powerful tools for studying the kinetics and dynamics of reactions involving charged or paramagnetic species. By perturbing the behavior of these species with rapid changes in electric or magnetic fields, researchers can gain valuable insights into reaction mechanisms, transient intermediates, and reaction rates

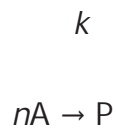
### **Flow Techniques**

The flow systems are generally of two types, viz. (i) plug flow in which there is no stirring in the reactor and (ii) stirred flow, in which there is stirring in the reactor to effect complete mixing within the reactor.

**(a) Plug Flow**

This is illustrated schematically as,

Let us consider a reaction of  $n$ th order with respect to reactant A as follows:



Then the rate of disappearance of substance is given by

$$\text{Rate of disappearance} = -dc/dt = kc^n$$

where  $c$  is the concentration of reactant at time  $t$ .

Let  $dv$  be an element of volume in the reactor.

Then,

$$\text{Rate of disappearance of reactant in a volume } dv = kc^ndv$$

After the system operates for a sufficient period of time, a steady state is established and three processes contribute to steady state as follows:

The molecules entering in reactor in time  $dt$ , i.e.  $ucdt$ , where  $u$  is the volume of rate of flow of reaction mixture passed through the reactor (liter per sec).

The molecules leaving the reactor in time  $dt$ , i.e.  $u(c + dc)dt$ .

The molecules disappearing by chemical reaction in time  $dt$  ( $-dn$ ). Also

$$-dn = kc^n dv/dt$$

The steady-state equation is obtained as follows:

Rate of entry of reactant = Rate of exit of reactant + Amount reacted

i.e. 
$$Uc/dt = u(c + dc)dt + kc^n dv/dt$$

$$\frac{d}{c} = k$$

or 
$$\frac{dc}{c} = \frac{k}{n} dv$$

If  $c_i$  and  $c_f$  are initial and final concentrations of reactant, then

$$\int_{c_i}^{c_f} \frac{dc}{c} = \frac{k}{n} \int v$$

$$-\int_{c_i}^{\bar{c}} \frac{dc}{u} = -k \int_0^V dv$$

where  $v$  is volume of the reactant. On integrating the above equation for  $n = 1$ , we get

$$\ln \frac{\bar{c}}{c_i} = -kV/u$$

or

$$c_f = c_i e^{-kV/u}$$

This equation may be compared by general first order equation,  $C = C_0 e^{-kt}$  and the quantity  $V_0 / u$  replaced by time, is known as *contact time for the reaction*. The contact time may be reduced by using high flow rate and small volume. The equation may be tested by varying  $V_0 / u$ , i.e. either by varying volume of reactor or the flow rate.

Equation can be written for  $n$ th order as

$$\frac{1}{n-1} \left( \frac{1}{c_f} - \frac{1}{c_i} \right) = \frac{kV}{u}$$

$$\begin{array}{r}
 n \quad u \\
 n \quad - \\
 -1 \quad 1 \\
 (n-1) \quad c_f \quad c_i
 \end{array}$$

The above equations are valid only when there is no volume change during the course of reaction.

### **(b) Stirred Flow**

The complete mixing in a stirred flow reactor has been discussed by Denbigh. In stirred flow, the composition becomes uniform throughout the entire volume of the reactor as a result of efficient stirring.

$$\text{Rate of flow of reactants into the reactor} = u c_i$$

$$\text{Rate of flow of reactants out of the reactor} = u c_f$$

$$\text{Rate of reaction in the reactor} = u c_i - u c_f$$

Also, Rate of reaction in the reactor =  $r \cdot V$ , where  $r$  is the rate per unit

volume and  $V$  the volume.

Therefore,

$$r \cdot V = u c_i - u c_f$$

or

$$r = u (c_i - c_f)/V$$

Thus, the measurement of  $c_i$  and  $c_f$  at a given flow rate  $u$  allows the reaction rate to be calculated from equation. The order of reaction and rate constant can be determined by carrying out experiments at different concentrations of reactants and rates of flow.

### **Continuous Flow Method**

In this method the reactants are forced into a mixing chamber and allowed to flow through a tube called *observation tube*. The analysis of reaction mixture is made at different points along the observation tube and thus the progress of the reaction at different times can be obtained.

The analysis can be made *in situ* using an optical, thermal, electrical or other method. The average time, during which the reaction proceeds before an element of volume and reaches a distance  $d$  along the reaction tube, is  $d/v$ , where  $v$  is the linear velocity. From the measurements made at various distances, a concentration time plot can be obtained from which the rate constant can be determined. Since the velocity of flow of the magnitude of  $10 \times 10^3 \text{ cm sec}^{-1}$  can be achieved, the shortest time interval for reaction that is accessible is of the order of  $10^{-3}$ sec.

### **Stopped-flow flash photolysis method**

The stopped-flow flash photolysis method is a powerful experimental technique used to study fast reactions, especially those involving short-lived intermediates and transient species. This method combines the stopped-flow technique with flash photolysis to monitor the kinetics of reactions initiated by a short and intense flash of light. Here's an overview of the stopped-flow flash photolysis method along with diagrams illustrating its principles:

### **Principle:**

### **Stopped-Flow Technique:**

- The stopped-flow technique involves the rapid mixing of two or more reactant solutions in a mixing chamber, followed by the immediate transfer of the mixed solution to a detection cell for analysis.
- The mixing process is typically controlled by pneumatics or hydraulics, allowing for extremely fast mixing on the millisecond to microsecond timescale.

### **Flash Photolysis:**

- Flash photolysis involves the use of a short and intense flash of light (usually from a xenon lamp or a laser) to initiate a photochemical reaction or to generate reactive intermediates.
- The flash of light excites or dissociates molecules in the reaction mixture, leading to the formation of transient species.

### **Stopped-Flow Flash Photolysis:**

- In the stopped-flow flash photolysis method, the reactant solutions are rapidly mixed in the mixing chamber, and immediately after mixing, a short and intense flash of light is applied to initiate the reaction or generate transient species.

- The reaction kinetics are then monitored by observing the transient changes in the absorbance or fluorescence of the reaction mixture over time.

### Experimental Setup:

#### Diagram:

#### Components:

1. **Syringe Pumps:** Used to deliver reactant solutions at controlled flow rates into the mixing chamber.
2. **Mixing Chamber:** The location where the reactant solutions are rapidly mixed.
3. **Flash Lamp:** Provides a short and intense flash of light to initiate the reaction or generate transient species.
4. **Detection Cell:** Where the mixed solution is transferred for analysis.
5. **Detector:** Measures the absorbance or fluorescence of the reaction mixture over time.
6. **Computer System:** Controls the operation of the syringe pumps, flash lamp, and detector, as well as data acquisition and analysis.

#### Procedure:

1. Reactant solutions are loaded into separate syringe pumps and delivered into the mixing chamber.
2. The syringe pumps rapidly mix the reactant solutions, and the mixed solution is immediately transferred to the detection cell.
3. A short and intense flash of light is applied to the mixed solution using the flash lamp, initiating the reaction or generating transient species.
4. The absorbance or fluorescence of the reaction mixture is monitored over time using the detector.



5. The resulting data are analyzed to determine the kinetics of the reaction, including the formation and decay of transient intermediates.

The stopped-flow flash photolysis method offers high temporal resolution and sensitivity, making it ideal for studying fast reactions and transient species in various fields such as chemical kinetics, photochemistry, and biophysics.